Richard Montgomery

Department of Mathematics University of California, Santa Cruz, CA 95064 USA rmont@ucsc.edu

https://people.ucsc.edu/ rmont/ Birthdate: July 22, 1956

EMPLOYMENT

7/2006- 9/2009: chair, Mathematics Department, University of California, Santa Cruz [UCSC]
9/1999-7/2020: Full Professor, UCSC.
7/1993-9/1999: Associate Professor, UCSC

7/1990-6/1993: Assistant Professor, UCSC

1988-1990 : NSF Postdoctoral Fellow taken at MSRI and University of California, Berkeley. 1986-1988 : Moore Instructor, M.I.T.

Some Visiting Positions

Aug.-Dec. 2018: Eisenbud Professor, Mathematical Sciences Research Institute, Berkeley, CA (semester in Hamiltonian Systems)

Sept.-Dec. 2014: Professor Invité, Institut Henri Poincaré, Paris France (trimester in subRiemannian Geometry)

2/2003: Astronome Invité, Bureau des Longitudes, Paris, France.

3/2001: Professeur Invité, Univerite de Boulogne, Dijon, France.

8/1997 to 7/1998: Visiting Professor, CIMAT, Guanajuato, Mexico.

6/1996: Professeur Invité, Universite de Geneve, Geneva, Switzerland

6/1992: Professeur Invité, Universite de Tours, France.

EDUCATION

1986-1988 Moore Instructor, Massachussets Institute of Technology [MIT] Cambridge, MA1986 Ph.D. Mathematics, University of California, Berkeley [UCB].1981 B.A. in Mathematics, B.A. in Physics, Sonoma State University. Sonoma, CA

GRADUATE AND POSTDOCTORAL ADVISERS

J. Marsden (U. C. Berkeley), V. Guillemin (MIT).

GRANTS

7/2020- present. Simons travel grant

7/2013-2016. NSF grant in the Mathematical Sciences [DMS-1305844]

7/2000- 2005. NSF grant in the Mathematical Sciences

1995-1997. (with M. Zhitomirskii of Technion, Haifa, Israel) Binational Science Foundation grant (joint US-Israel)

6/1997-5/2000. (with V. Ginzburg, UCSC) NSF grant in the Mathematical Sciences.

7/1994-6/1997. NSF grant in the Mathematical Sciences

6/1992-5/1994. (with T. Ratiu and D. Lewis, UCSC) NSF grant in the Mathematical Sciences.

AWARDS

2012: Fellow of American Mathematical Society.
2001-2003: Sigma-Xi distinguished lecturer.
8/1994-12/1994: Fulbright Fellowship to the United Kingdom.
1988-1991: Postdoctoral Fellowship, NSF.

PUBLICATIONS

IN JOURNALS

1. "Canonical Formulations of a Particle in a Yang-Mills Field and Wong's Equations", Lett. Math Phys., vol. 8, pp. 59-67, 1984

2. "Analytic Proof of Chaos in the Leggett Equations for Superfluid He3", J. Low Temp. Phys, vol. 58, no. 5/6, pp. 417-423, 1985

3. "Scattering Off of an Instanton", Comm. Math. Phys., vol. 107, pp. 515-533, 1986

4. (with D. Lewis, J. Marsden, and T. Ratiu) "The Hamiltonian Structure for Dynamic Free Boundary Problems", Physica D, vol. 18, pp. 391-404, 1986

5. (with J. Marsden, P. Morrison, and W.B. Thompson) "Covariant Poisson Brackets for Classical Field Theories", Annals of Physics, vol. 169, pp. 29-48, 1986

6. "Corrections to the Low-Energy Scattering of Monopoles", Physics Letters A, vol. 125, no. 4, pp. 159-161, 1987

7. (with N. Ercolani, G. Forest, and D. McLaughlin) "Hamiltonian Structure of Modulation Equations for Sine-Gordon", Duke Math Journal, vol. 55 no. 4, pp. 949-983, 1987

8. (with L. Bates) "Closed Geodesics on the Space of Stable Two-Monopoles", Comm. Math. Phys. vol. 118, no. 4, pp. 635-640, 1988

9. "The Connection for a Family of Completely Integrable Systems whose Holonomy is the Classical Adiabatic Angle (Berry's phase)", Comm. Math. Phys., vol. 120, pp. 269-294, 1988

10. (with J. Marsden and T. Ratiu) "Cartan-Hannay-Berry Phases and Symmetry", Cont. Math., vol. 97, pp. 279-296, 1989

11. "Isoholonomic Problems and Some Applications", Comm. Math. Phys., vol. 128, pp. 565-592, 1990

12. "How Much Does the Rigid Body Rotate? -a Berry's Phase from the 18th Century", Am. J. Physics, vol. 59, no. 5, pp. 394-398, 1991

13. "Generic Distributions and Lie Algebras of Vector Fields", Journal of Differential Equations, vol. 103, no. 2, pp. 387-393, 1993

14. (with Nicholas Ercolani) "On the Fluid Approximation to a Nonlinear Schrodinger Equation", Physics Letters A, vol. 180, no. 6, pp. 402-408, 1993

15. "Abnormal Minimizers", SIAM J. Control and Optimization, vol. 32, no. 6, pp. 1605-1620, 1994

16. "Singular Extremals on Lie Groups", Math. Control Signals Systems, vol. 7, no. 3, pp. 217-234, 1994

17. "Hearing the Zero Locus of a Magnetic Field", Communications in Mathematical Physics, vol. 168, no. 3, pp. 651-675, 1995

18. "A Survey of Singular Curves in Subriemannian Geometry", vol. 1, Journal of Dynamical and Control Systems, 1995

19. (with K. Ehlers, A. Samuel, and H. Berg) "Do Cyanobacteria swim using travelling surface waves?", Proceedings of the National Academy, Biophysics section, vol. 93, no. 16, pp. 8340-8343, Aug. 6, 1996

20. (with B. Shapiro and M. Kazarain), "Characteristic Classes for the Degenerations of Two-Plane Fields in Four Dimensions", Pac. J. Math., vol. 179, no. 2, pp. 355-370, 1997

21. (with K. Ehlers and J. Koiller) "Problems and Progress in Microswimming", J. Nonlinear Science, vol. 6, pp. 507-541, 1996

22. "The Geometric Phase of the Three-Body Problem", Nonlinearity, vol. 9, no. 5, pp. 1341-1360, 1996

23. "The N-body problem, the braid group, and action-minimizing periodic orbits", Nonlinearity, vol. 11, no. 2, pp. 363-376, 1998

24. Book review of "Global Aspects of Classical Integrable Systems", by L. Bates and R. Cushman, SIAM Review, March, pp. 164 - 167, 1998

25. (with J. Koiller, M.A. Raupp, J. Delagado, and K.M. Ehlers) "Spectral Methods for Stokes Flows: the Lorentz Operator", Comp. Appl. Math., vol. 17, no. 3, pp. 343-371, 1998

26. (with V. Ginzburg) "Geometric quantization and no-go theorems", Banach Center Publ. vol. 51, (Poisson Geometry), Polish Acad. Sci, Warsaw, 2000

27. Featured Math Review (solicited; on the AMS web page) of M. Gromov's "Carnot-Caratheodary Spaces seen from within", May 2000

28. "A remarkable periodic solution of the three-body problem in the case of equal masses", with Alain Chenciner, Annals of Mathematics, **152**, pp. 881-901, 2000

29. "A new solution to the three-body problem", Notices of the American Mathematical Society, vol. 48, no. 5, pp. 471-481, 2001

30. "Geometric approach to Goursat flags" (with M. Zhitomirskii), Ann. Inst H. Poincare Anal. Non Linéare, vol. 12, no. 4, pp. 459-493, 2001

31. "Infinitely many syzygies", Archives for Rational Mechanics and Analysis, vol. 164, no. 4, pp. 311-340, 2002

32. (invited book review) "Symmetry in Mechanics: A Gentle, Modern Introduction, by Stephanie Singer," American Math. Monthly, April, 2003

33 (with M. Shapiro and A. Stolin) "A nonintegrable sub-Riemannian geodesic flow on a Carnot group", J. Dyn. Control Systems, vol. 3, no. 4, pp. 519 - 530, 1997

34. "Fitting hyperbolic pants to a three-body problem". Ergodic Theory Dynam. Systems v. 25 no. 3, pp. 921-947, 2005,

35. (with Alain Chenciner and Jacquez Féjoz)" Rotating eights. I. The three Γ_i families", Nonlinearity v. 18, no. 3, pp. 1407-1424, 2005.

36. (with Toshiaki Fujiwara) "Convexity of the figure eight solution to the three-body problem", Pac. J. Math., no. 2, vol. 219, 271-285, April 2005.

37. (with Alex Castro, Roberto Manduchi, and X. Shi) "Rotational Invariant Operators Based on Steerable Filter Banks" IEEE Signal Processing Letters, vol. 13, no. 11, Nov. 2006

38. (with Persi Diaconis and Susan Holmes) "Dynamical Bias in the Coin Toss", (featured article), SIAM Review, Vol. 49, no. 2, pp. 211-235, May 2007.

39. "The zero angular momentum, three-body problem: all but one solution has syzygies", Ergodic Theory Dynam. Systems, vol. 27, no. 6, pp. 1933-1946, 2007.

40. (with Duncan Ralph, and Onuttom Narayan) "Exact identity for nonlinear wave propagation", Physical Review E, vol. 77, 056219, May 2008.

41. (with Alex Castro) "The Chains of Left-invariant CR-structures on SU(2)", Pac. J. Math., vol. 238, no. 1, 41-71 2008.

42. (with Vidya Swaminathan and Michail Zhitomirskii) "Resolving Singularities Using Cartan's Prolongation", Journal of Fixed Point Theory and Applications (Arnol'd volume), vol. 3., no. 2, August 8, 2008 (online).

43. (with Sam Kaplan and Mark Levi) "Making the moon reverse its orbit: stuttering in the planar three body problem", in Discrete and Continuous Dynamical Systems series B, (Sim-fest issue), vol. 10, no. 2/3, 2008.

44. (with Gil Bor) " G_2 and the Rolling Distribution", L'Enseignement Mathematique, vol. 55, pp. 157-196, 2009

45. "Sub-Riemannian geometry: general theory and examples", invited book review. Bull. Amer. Math. Soc., vol. 47, pp. 713-722, 2010

46. (with AL Castro) "Spatial curve singularities and the Monster/Semple tower", Israel Journal of Mathematics, vol. 192, no. 1, pp. 381-427, 2012.

47. (with R. Moeckel and A. Venturelli), "From Brake to Syzygy", Archive for Rational Mechanics and Analysis; vol 204, no. 3, pp. 1009-1060, 2012.

48. (edited by T. Ratiu and A. Weinstein) in 'Remember Jerry', Notices of the AMS, vol. 59, no. 6, p. 767, 2012

49. (with R. Moeckel), "Symmetric Regularization, Reduction, and Blow-Up of the Planar Three-Body Problem", Pac. J. Math., vol. 262, no. 1, 2013

50. (with Gil Bor) "Poincare y el problem de N-cuerpos", in Miscelánea matemática de la Sociedad Matemática Mexicana, May issue, no. 57 'extraordinario', 2013

51. (with Corey Shanbrom) "Keplerian Motion on the Heisenberg Group and Elsewhere" in Geometric Mechanics: The Legacy of Jerry Marsden, Fields Institute Communications Series, 2015

52. "MICZ-Kepler= Dynamics on the Cone over the Rotation Group", Regular and Chaotic Dynamics November 2013, Volume 18, Issue 6, pp. 600-607, 2013

53. "The Three-body problem and the shape sphere", Amer. Math. Monthly, vol. 122, no. 4, pp. 299-321, April 2015.

54. "Who's a fraid of the Hill boundary? -conjugate loci clustering at the boundary", <code>SIGMA</code> vol. 10 2014

55. (with R. Moeckel), "Realizing All Reduced Syzygy Sequences in the Planar Three-Body Problem", Nonlinearity, vol. 28 pp 1919-1935, 2015

56. (with Enrico Le Donne, Alessandro Otazzi, Pierre Pansu, and Davide Vittone) "Sard Property for the Endpoint Map on some Carnot Groups', Ann. de l'Inst. Henri Poincaré C- Analyse non linéaire, vol. 33, no. 6, pp. 1639-1666, Nov.-Dec. 2016

57. (with Holger Dullin) "Syzygies in the two center problem", Nonlinearity, vol. 29, no. 4, 2016

58. (with Connor Jackman) "No Hyperbolic Pants for the Planar Four-Body Problem", Pacific Journal of Mathematics vol. 280, no. 2, pp 401-410, 2016

59. (with Jacques Féjoz and Andreas Knauf) "Lagrangian Relations and Linear Point Billiards", Nonlinearity, vol. 30, no. 4, 2017

60. "Constructing the Hyperbolic Plane as the reduction of a three-body problem", Regular and Chaotic Dynamical Systems, no. 6, vol. 22, 2017.

61. (with R. Moeckel and H. Sanchez), "Free time minimizers for the planar three-body problem", Celestial Mechanics and Dynamical Astronomy, vol. 130, no. 3, article 28 (on-line version), 2018

62. 11Oscillating about Coplanarity in the 4 body problem", Inventiones Math. , Inventiones mathematicae, vol 218(1), 113-144, 2019.

63. (with J-H Cheng, T Marugame, V. Matveev) "Chains in CR geometry as geodesics of a Kropina met-

ric", Advances in Mathematics, vol. 350, pp. 973-999, 2019 (online: https://doi.org/10.1016/j.aim.2019.05.004) 64. "The Three-Body Problem", Scientific American, August 2019.

65. (with N. Duignan, R. Moeckel, and Guowei Yu), "Chazy-Type Asymptotics and Hyperbolic Scattering for the *n*-Body Problem", Arch. Rat. Mech, 2020

66. (with Andrey Ardentov, Gil Bor, Enrico Le Donne, and Yuri Sachkov), "Bicycle paths, elasticae and sub-Riemannian geometry", Nonlinearity, vol. 34, no. 1, pp. 4661-4683, June 2021

67. (with O. Narayan and H. Mathur) "Evading Anderson localization in a one-dimensional conductor with correlated disorder", Phys Rev B, vol. 103, 144203, April 2021

68. (with Jacques Fejoz and Andreas Knauf) "Classical n-body scattering with long-range potentials", Nonlinearity, vol. 34, no. 11, pp. 8017- 8054, Oct. 14, 2021

69. (with Alejandro Bravo Doddoli) "Geodesics in Jet Space", Reg and Chaotic Dyn., vol. 27, no. 2, pp. 151-182, 2022

IN BOOKS OR CONFERENCE PROCEEDINGS.

1. (with J. Marsden and T. Ratiu) "Gauged Lie-Poisson Structures", Contemp. Math., vol. 28, 101-114, 1985.

2. (with J. Marsden and T. Ratiu) "Reduction, Symmetry, and Phases in Mechanics", Memoirs of the AMS, vol. 88, 1990.

3. (with G. Bor) "SO(3) Invariant Yang-Mills Fields which are Not Self-dual", in Hamiltonian systems, Transformation Groups and Spectral Transform Methods (J. Harnad and J. Marsden, editors), 191-198, Les Presses de l'Université de Montreal, 1990.

4. "Optimal Control of Deformable Bodies and Its Relation to Gauge Theory", in The Geometry of Hamiltonian Systems MSRI publications, vol. 22, 403-438, Springer-Verlag, 1991.

5. "Heisenberg and Isoholonomic Inequalities", in Symplectic Geometry and Mathematical Physics, proceedings in honor of Jean-Marie Souriau, ed. by P. Donato, Progress in Mathematics, vol. 99, 303-325, Birkhauser, Boston, 1991.

6. "Nonholonomic Control and Gauge Theory", in Nonholonomic Motion Planning, (J. Canny and Z. Li, editors), Kluwer Acad Press, 343-378, 1993.

7. "Gauge Theory of the Falling Cat", in Dynamics and Control of Mechanical Systems, M. Enos, ed., Fields Institute Commun., 1, 193-218, AMS, 1993.

8. (with Eugene Lerman and Reyer Sjamaar) "Examples of Singular Reduction", in Symplectic Geometry, ed. by D. Salomon, London Math. Society Lecture Note Ser., 192, 127-155, Cambridge University Press, 1993.

9. (with S. Sastry) "The structure of optimal control for a steering problem", Nonlinear Control Systems Design 1992. Selected Papers from the 2nd IFAC Symposium. (Nonlinear Control Systems Design 1992). Edited by M. Fliess, Pergamon Press, UK, 135-140, 1993.

10. "Abnormal Optimal Controls and Open Problems", Nonlinear Control Systems Design 1992. Selected Papers from the 2nd IFAC Symposium. (Nonlinear Control Systems Design 1992). Edited by M. Fliess, Pergamon Press, UK, 1993.

11. "Survey of Singular Geodesics", in Subriemannian Geometry, in Progr. Math. vol. 144, 325-339, Birkhauser, 1996.

12. "Introduction to a paper of M.Z. Shapiro: Homotopy theory in Control", in Nonsmooth analysis and geometric methods in deterministic control, The IMA Vol. Math. Appl. vol. 78, Springer-Verlag, 1996.

13. "Engel Deformations and Contact Structures", Amer. Math. Soc. Transl., (2) vol 196, 103-117, 1999.

14. (with A. Cherman, J. Delgado, F. Duda, K. Ehlers, and J. Koiller) "Low Reynolds number swimming in two dimensions" in Hamiltonian systems and celestial mechanics (Patzcuaro, 1998)', 32–62, World Sci. Monogr. Ser. Math., 6, World Sci. Publishing, River Edge, NJ, 2000.

15. "A tour of subriemannian geometries, their geodesics, and applications". [monograph], Mathematical Surveys and Monographs, vol. 91, American Math. Society, Providence, Rhode Island, 2002.

16. "Action spectrum and collisions in the planar three-body problem", in Contemporary Math. vol. 292 (Celestial Mechanics), American Math. Society, Providence, Rhode Island, 2002.

17. (with A. Chenciner, J. Gerver, C. Simó) "Simple Choreographic Motions of N bodies: A preliminary study", in Geometry, Mechanics, and Dynamics, volume in honor of the 60th birthday of J.E. Marsden, P. Newton, P. Holmes, A. Weinstein, ed., Springer-Verlag, 2002.

18. (with J. Koiller, W. Earnest, Joaquin Delgado, K. Ehlers, T. Stuchi, Maria de Fatima Almeida) "Momentum maps and geometric phases", in Classical and celestial mechanics, (Recife, 1993/1999), 281– 349, Princeton Univ. Press, Princeton, NJ, 2002.

19. (with K. Ehlers, J. Jair, and P. Rios) "Nonholonomic systems via moving frames: Cartan equivalence and Chaplygin Hamiltonization" in The breadth of symplectic and Poisson geometry, 75–120, Progr. Math., 232, Birkhuser Boston, Boston, MA, 2005.

20. "The Three Body Problem, A Cambridge Mystery", Notices of the AMS, invited book review, 1031-1033, Oct. 2006.

21. (with Michail Zhitomirskii) "Points and Curves in the Monster Tower", Memoirs of the A.M.S., vol. 205, 2010.

22. (with Corey Shanbrom) "Keplerian Dynamics on the Heisenberg Group and Elsewhere", to appear: Geometry, Mechanics and Dynamics: The Legacy of Jerry Marsden, Fields Institute Communications series, 2013.

23. "Blow-Up, Homotopy and Existence for Periodic Solutions of the Planar Three-Body Problem", in **Geometrical Themes Inspired by the N-body Problem**, Springer LNM 2204, L. Hernández-LaMondea, H. Herrera, and R. Herrera editors, 2018.

STUDENTS.

UNDERGRADUATE.

Matt Chisholm. Mentored for Steck award and undergraduate thesis. 1999-2000. Kevin Vajk. Undergraduate thesis. 1995.

PhD STUDENTS.

Gil Bor, (1991) co-advised with J. Marsden, UCB All my other students received their PhD from UCSC. Pat Tantalo, (1993) co-advised with T. Ratiu Girija Mittagunta, (1994) co-advised with T. Ratiu Kurt Ehlers, (1996) . Andrew Klinger, (1999). Alexander Golubev, (1999), co-advised with Viktor Ginzburg. Cesar Castilho, (1999), co-advised with Viktor Ginzburg William C. McCain (2007) Vidya Swaminathan (2008) Alex Castro (2010) Corey Shanbrom (2013) Wyatt Howard (2013) Connor Jackman (2018) Gabriel Martins (2018) Sean Gasiorek, (2018) Steven Flynn, (2020) Andres Perico (2021)

COLLABORATORS.

A partial list of collaborators, in rough reverse chronological order. University affiliations are in parends and tend to be current affiliations. All are co-authors for papers appearing in refereed journals. When affiliation is not with a math department, then the person's department is stated at the line's end.

Rick Moeckel (U. Minn.) Hector Sanchez (UNAM, Mexico City) Andreas Knauf (Nürmberg-Erlangen, Germany) Onuttom Narayan (UCSC) physics Roberto Manduchi, (UCSC) Electrical Engineering and Computer Science. Persi Diaconis, (Stanford) Math. + Statistics. Susan Holmes, (Stanford) Statistics Toshiaki Fujiwara, (Kitasato University, Japan) Alain Chenciner, (Bureau des Longitudes and Paris 7, Paris) Carles Simó, (U. of Barcelona) Mikhail Zhitomirskii, (Technion, Haifa) Joseph Gerver, (Rutgers U., Camden Campus, N.J.) Jair Koiller, (Federal University, and Laboratorio Nacional de Computação, Rio de Janiero) K. Ehlers, (Reno Community College, Reno, Nevada.) Boris Shapiro, (U. of Stockholm) Howard Berg, (Harvard, and the Rowland Institute, Cambridge; deceased) Biology Dept. Viktor Ginzburg, (UCSC) Shankar Sastry, (UC Berkeley) Electrical Engineering and Computer Science Zexiang Li, (UC Berkeley) Electrical Engineering and Computer Science Tudor Ratiu, (UCSC) J.E. Marsden, (UC Berkeley; deceased) Nick Ercolani, (U. of Arizona, Tucson) Greg Forest, Mathematics (U.N.C, Chapel Hill, NC) Dave McGlaughlin, (NYU) D. Lewis, (UCSC) Larry Bates, (U. of Calgary) Eugene Lerman, (U. of Ilinois, Champagne-Urbana) Reyer Sjamaar, (Cornell)

UNIVERSITY SERVICE.

Department of Mathematics.

Fall 1990. Organized and administered the Putnam Exam (national undergraduate mathematics competition).

1990-91. Undergraduate Vice-Chair for department advising and signing forms (Winter/Spring) for mathematics majors; matriculation agreements

Spring 1991. graduate geometry seminar

1991. Member of Department Library Committee

1991-1992. graduate geometry seminar

1991-1992. Member, Department Recruitment Committee.

1991-1992. Undergraduate Vice-Chair for department advising and signing forms for mathematics majors; matriculation agreements

1993-1994. Graduate Vice-Chair for department advising and signing forms for mathematics graduate students

1993-1994. Recruited two foreign graduate students with full support: Cesar Castilho; funded by CNPq, Brazil Juan-Pablo Ortega; funded by Fulbright/Rotary Scholarship, Spain

1995-1998: Graduate Vice-Chair for department

2002-3: Chair of committee for restructuring graduate program.

2004-5: Cochair with A. Tromba.

2006-9. Department chair.

Division of Natural Sciences.

1991. 1992, 1999. Science Day.
1997-2000. Applied Mathematics committee. (Charged with starting that department)
2000-2002: member of Divisional CAP
2002-2003: chair of Divisional CAP
2015-2016: Divisional CAP member

Campuswide Academic Senate

1999,2001,2002. Member of Ad-hoc committees. 2018-2019. Senate comittee on Educational Policy ['CEP']

OUSTSIDE PROFESSIONAL ACTIVITES.

Invited Lectures.

4/1990 Symplectic Geometry Seminar, Stanford University

5/1990 Mathematical Physics Seminar, Utrecht, The Netherlands

5/1990 Mathematics Colloquium, University of California at Berkeley

6/1990 Mathematical Physics Seminar, Heidelberg, Germany

6/11-15/1990 Colloque International en l'honneur de Jean-Marie Souriau 'Geometrie Symplectique et Physique Mathematique' Aix-en-Provence, France.

6/25-30/1990 Conference in Nonlinear Elasticity, Oberwolfach, Germany

7/29/1980 through 8/3/1990 Conference on Topological Phases in Nuclear and Molecular Systems, organized by Alden Meade (physical chemist, Telluride, Colorado

11/1990 Mathematics Colloquium, University of Arizona at Tucson

12/1990 Differential Geometry Seminar, University of California at Berkeley

3/1992 Conference on Falling Cats and Other Nonholonomic Systems Fields Institute, Canada

7/1992 Conference on Subriemannian Geometry, Paris 6, Paris, France

4/1992 AMS conference on Symplectic Topology, Fayetteville, Arkansas

5/1992 UC Davis Mathematics Colloquium, University of California, Davis

6/1992 Conference on Variational Principles and Nonholomic Control Fields Institute, Canada.

6/1992 Conference on Nonlinear Control, Bordeaux, France

7/1992 Conference on Subriemannian Geometry, Paris, France

3/1994 MSRI workshop on Differential Systems, Submanifolds, and Control, talk entitled "Hearing Singular Extremals", Berkeley, California

3/1994 "Gauge Theory and Swimming Micro-organisms", Caltech, California

9/1994 "Is there time-periodic monopole motion?" Spital fields Day Conference, sponsored by the London Mathematical Society, held at the Isaac Newton Institute of Mathematical Sciences, Cambridge, England

3/1995 "Subriemannian Volumes", Pacific Northwest Geometry Seminar 1995 Winter Meeting, held at the Mathematical Sciences Research Institute, Berkeley, California

4/1995 "Isoperimetric Problems and Falling Cats" Colloquium, Sonoma State University

4/1995 "Geometric Phase in the 3 Body Problem", University of Arkansas Spring Lecture Series

6/1995 "Geometric Phase in the 3 Body Problem", IMPA, Rio de Janeiro, Brazil

6/1995 Workshop on Biological Motion, CNPq, LNCC, Rio de Janeiro, Brazil

7/1995 ARO-NASA Montana State University Workshop on Intelligent Control Conference on Nonlinear Control and Robotics

4/1996 "Geometric Phase in the three-body problem", U.C. Berkeley Differential Geometry Seminar

9/14/1996: Washington DC. workshop in Biology and Control for the NSF , "Mystery swimmers: How Cyanobacteria swim". Workshop in "Biology and Control" for the NSF in Washington DC.

11/1996 "Singular Curves and a Sard Theorem in Subriemannian Geometry", 1996 Fall Western Sectional Meeting of the AMS, Pasadena, CA

12/29/1996: -Jan. 7 1997: International Conference on Singularities and Control Theory, Technion, Haifa, Israel, "A survey of singular geodesics in subriemannian geometry".

11/1997 "The braid group and periodic orbits for the N-body problem", in the Celestial Mechanics session of the joint SMM-AMS meeting in Oaxaca, Mexico.

1/13/98 "Grupo de trenzas y el problema del N cuerpos", UAM, Ixtapalapa, Mexico City

1/15/98 "Teoria de normas en controle optimo", in UAM, Acapatulco, Mexico City

4/9/98 "Orbitos periodicos por el problema del N cuerpos en el plano", CIMAT, Guanajuato, Mexico.

3/18/98 "(4,7) distributions: a case study, I", seminaire de controle, Institut Henri Poincare Universite Pierre et Marie Curie, Paris, France

3/20/98 "(4,7) distributions: a case study, II", seminaire de controle, Institut Henri Poincare Universite Pierre et Marie Curie, Paris, France

3/26/98 "The Braid Group and action minimizing periodic orbits", Bureau de Longitudes, seminaire de mecanique celeste.

4/3/98 "A survey of problems and results in Subriemannian geometry", Institut Henri Poincare Universite Pierre et Marie Curie seminaire en geometrie symplectique de C. Marle

4/26/98 "Quaternionic contact distributions and their symmetry groups", MIT, symplectic geometry seminar, MIT, Cambridge, MA.

5/1/98 "The braid group and periodic orbits in the planar N-body problem", gauge theory seminar, Harvard U. Cambridge, Mass.

8/2-7/98 Mecanica Celestial for the Curso de Verano (summer school for the year between undergraduate and master's level students) CIMAT, Guanajuato, Mexico

12/16/1999: Northwestern U., Evanston, Ill, USA ; International Conference in Celestial Mechanics in honor of Don Saari's 60th birthday: "Figure eights with three bodies".

3/2/00 "Figure eights with three bodies", UC Berkeley, math colloquium.

4/9/00 "A Tour of the zoo of Distribution", AMS conference, Notre Dame.

4/20/00 "Figure eights with three bodies", Stanford University, math colloquium.

5/22/00 "Figure eights with three bodies", UC Davis, math colloquium.

5/24/00 "Figure eights and flowers with n-bodies", CalTech, Control and Dynamical Systems colloquium.

5/20/2001 "New solutions to the three-body problem", , Park City Utah, **plenary talk** for the SIAM Dynamics Days conference.

6/20/200 2"New solutions to the N-body problem", Portland, OR, plenary talk for the AMS meeting.

10/16/2002, "New solutions to the N-body problem", Sonoma State U. Math colloquium, Rohnert Park, CA.

11/17/2002, "Variational Methods in the N-body Problem". Pacific Northwest Geometry Seminar at Oregon State University,

2/14/2003 "The three body problem" a general science audience talk, Contra Costa community college, (Sigma-Xi lecturer).

3/6/2003 "Conformal Structure of the Shape Sphere" Bureau des Longitudes, Paris, France.

3/20/2003 "Scattering in the three-body problem", Bureau des Longitudes, Paris, France.

6/10/2003 Introductory Talk for the start of the AIM/ARCC international conference on Variational Methods in Celestial Mechanics.

6/12/2003 "Infinitely Many Syzygies and the conformal structure of the shape sphere", AIM/ARCC international conference on Variational Methods in Celestial Mechanics.

1/7/2005, Phoenix Arizona, AMS/MAA Joint Mathematics Meeting, special session in Celestial Mechanics, "Bifurcations out of the Eight".

3/15/2004 "Falling Cats, planets, and gauge theory", a general science audience talk, Presentation High School, San Jose California, honors society.

4/18/2004, "Fitting hyperbolic pants to a three-body problem", Banff, Canada, BIRS workshop on celestial mechanics.

4/27/2004, "Why coin flipping is biased", a general science audience talk, Long Beach State University, Sigma-Xi invited lecture.

4/29/2004,"Dynamical Bias in Coin-Flipping", UC Santa Cruz Physics Colloquium, U.C. S.C, Santa Cruz, CA.

12/14/2004. "Dynamical Bias in Coin Tossing", Mathematics colloquium, Nara Woman's University, Nara, Japan,

12/13/13-15, 2004. Three one hour lectures (mini-course) on subRiemannian Geometry, in the Workshop on subRiemannian geometry, Nara Woman's University, Nara, Japan,

12/17-18/2004, Two one-hour lectures on new solutions to the N-body problem, in the Workshop on Dynamical Systems. Kyoto University, Kyoto, Japan.

4/1/2005, "Fitting hyperbolic pants to a three-body problem", Minneapolis MN, Midwest dynamical systems meeting.

4/9/2005, "Around the eight", International Conference in Honor of Don Saari, CIMAT, Guanajuato, Mexico.

9/7/2005 "Prolongations of Lie algebras and Symmetries of Distributions" Math Colloquium, San Jose State University.

10/4/2005. "A new characterization of an orbit of Lagrange" UCSC Math colloquium.

10/26/2005 "Fitting hyperbolic pants to a three-body problem" Dynamical Systems Seminar, Penn State, State College, PA.

10/27/2005 "The N-body problems" MASS undergraduate colloquium, Penn State, State College, PA.
 10/27/2005 "The N-body problem. New solutions. new problems" math colloquium, Penn State, State

College, PA.

11/9/05 "Bias in Coin-flipping," undergraduate mathematics colloquium. UCSC.

4/29/06 "G2 and rolling" invited talk, AMS special session on Elliptic methods in geometry, SF State.

4/29/06 "Infinitely many syzygies, redux" - invited talk, AMS special session on Geometry dynamics and Ergodic Theory , SF State.

5/18/06 "Stuttering in the three-body problem" - invited talk, colloquium, Bureau des Longitudes Seminar, Paris, France.

5/19/06 "G2 and rolling" geometry colloquium, Paris VII, Paris, France

5/29/06 "Only Lagrange is Syzygy-Free", conference in honor of Carles Simo's 60th birthday, S'agaro, Spain.

1/31/06 "G2 and the rolling distribution", invited speaker at BIRS, in Banff, the workshop on "Non-holonomic Dynamics and Integrability" held Jan. 28- Feb 2, 2007.

5/10/07 "Scattering in the N-body problem", invited talk at the 38th annual meeting of the American Astronomical Society's Division of Dynamical Astronomy, Ann Arbor, MI, held May 6-10.

6/8/07 "Scattering in the N-body problem" in the conference "Symmetry and Perturbation Theory" held June 2-9 June 2007 in Otranto (Puglia, Southern Italy)

5/6/08-5/09/08 "Singularities of 2-plane fields, Legendrian Curves, and the Friendly Monster" an invited mini-course given at the Centre de Recherches Mathematiques, Universite de Montreal.

12/6/08 "Resolving Curve Singularities and Higher Contact Manifolds", invited lecture at the 1st meeting of the Bay Area Differential Geometry Seminar, (held at MSRI).

9/23/2009 "Compactifying Taylor Series" undergraduate math colloquium, U. N.C., Asheville.

2/6/2009 "From the Falling Cat to Celestial Mechanics", math colloquium, University of Milano-Bicocca, Milan, Italy.

3/4-3/7/2010 "Variational Methods in Celestial Mechanics', a series of four lectures in an NSF-sponsored graduate mini-school in Celestial Mechanics, at U. of Maryland, College Park, MD.

3/30/2010 "Goursat distributions, Monster/Semple Towers and Algebraic Geometry" in 'New Trends in Sub-Riemannian geometry', a conference held in Nice, France from 3/29-4/2/2010

4/8/2010 "Ubiquity of Stuttering" Bureau des Longitudes, Paris, France.

7/4-7/8/2011: A 5 day summer school in Geometric methods in the N-body problem as one of the three teachers for 5th Summer School in Geometry, Mechanics and Control in Spain. (Miraflores de la Sierra, near

Madrid.)

7/13/2011. "The Brake-to-Syzygy Map in the planar three-body problem" invited lecture, Universitat Politcnica de Catalunya, Barcelona, Barcelona, Spain.

 $10/03/2011.\,$ "K3 and the planar four body problem". In the Floer Memorial Lecture, a yearly lecture at UC Berkeley in honor of Andreas Floer.

 $10/13/2011.\,$ "From the planar four-body problem to the K3 surface" invitied lecture at the IAS in Princeton.

3/26/2012: "From Brake to Syzygy in the three-body problem" IAM-PIMS-MITAC distinguished colloquium series, UBC, Vancouver, British Columbia, Canada

3/28/2012: "Reducing and regularizing everything for the N-body problem", Applied Math. Colloq., U. Victoria, Victoria, British Columbia, Canada.

7/25/2012 Plenary speaker, "Regularizing and reducing the whole shebang", Marsdenfest, Fields Institute, Toronto, Canada.

12/13-14/2012 Invited speaker, "Variational and Geometric approaches to N body problems", Poincaré Symposium (honoring the 100th anniversary of Poincaré's death), Brown University, Providence RI.

1/15/2013, Invited speaker "Paradoxes and Opportunities from Global Regularization", Banff ?International Research Center weeklong program "New Perspective on the N-body problem."

4/15/2013. Colloquium speaker "The Three-Body Problem: Open problems, new solutions and the shape sphere of triangles." Mathematics Dept., Reed College.

4/11/2014. Invited speaker "From the falling cat to the N-body problem' International conf on Geometry, Control, and Mechanics, IMPA, Rio de Janeiro.

4/14/2014. Colloquium "Two open problems in the N-body problem", Departmento de Mathematica, Universidade Federal de Sergipe, Brazil.

4/16/2014. Special Lecture Series: "From falling cats to the 3-body problem", Departmento de Mathematica, Universidade Federal de Pernambuco, Brazil.

4/17/2014. Colloquium spearker "Regularizing and Reducing Everything", Departmento de Mathematica, Universidade Federal Rural de Pernambuco, Brazil.

5/03/2014. Invited speaker, 'Differential geometry arising from the N-body problem.' Pacific Northwest Geom Seminar, yearly meeting, Eugene, OR

5/07/2014. Colloquium speaker, "The Kepler-Heisenberg problem", U. of Washington Mathematics Colloq., Seattle, WA.

9/29/2014. Invited speaker, "Searching for Area rules in nonAbelian gait generation", international workshop on Geometric Analysis on subRiemannian Manifolds, Institut Henri Poincaré, Paris, France.

10/30/2014, Invited speaker, "Sketch of the Syzygy Program", dynamics seminar, Universidad Autonoma de Barcelona, Barcelona, Spain.

11/6/2014.Colloquium speaker, "Particles in Magnetic Field. Abnormal Minimizers in Geometry", Bureau des Longitudes (IMCEE), Paris France

11/12/2014. Colloquium speaker, "Solutions for the three-body problem realizing every free homotopy class", applied dynamical systems colloquium, Imperial College, London, U.K.

11/24/2014, plenary speaker, "Reduction and Singular Curves", International Conference Honoring the 80th Birthday of Charles Marle, Institut Henri Poincaré, Paris, France.

11/26/2014. Invited speaker, "Open Problems in subRiemannian Geometry", international workshop on Nonholonomic Mechanics and Optimal Control, Institut Henri Poincaré, Paris, France.

12/4/2014. Colloquium speaker, "From Falling Cats to Quantum Mechanics near the zero locus of a Magnetic Field", Institut Fourier, (mathematics department) Univ of Grenoble, Grenoble, France.

12/10/2014. Invited speaker, "A Tale of Two Towers", international workshop on Equivalence, invariants, and symmetries of vector distributions and related structures : from Cartan to Tanaka and beyond, Institut Henri Poincaré, Paris, France.

10/26/2015. Undergraduate Colloquium, "Geometry and Billiards", UCSC.

4/12/2016: invited speaker "The Shape Sphere: A New Vista on the Three-body problem", 17th conferencia David Alcaraz, IIMAM, UNAM, Mexico City, Mexico. (a single public lecture given once a year or less often, in honor of David Alcaraz, a mathematician at UNAM who died in the 1985 earthquake there).

 $5/16/2016\colon$ undergraduate mathematics colloquium "Quantum mechanics and projective geometry" , UCSC.

3/13/2017: talk in UCSC Math Club, "Heisenberg Groups" undergraduate mathematics colloquium.

4/5/2017: talk at Penn State, Applied Analysis Seminar: "When Parabolic Minimizers all tend to Lagrange in the three-body problem".

11/9/2017: AIM international conference on PseudoHermitian Geometry, invited talk: "The Kepler Problem on the Heisenberg Group"

12/5/2017: UCSC Math Colloquium: "Mechanics and Mnev's Universality Theorem"

01/11/2018, AMS Joint Meeting, San Diego, AMS Special Session on New Trends in Celestial Mechanics, I : "Metric Geometry and Marchal's lemma"

03/28/2018: U. of Maryland Math Colloquium, "Overview of my work on the N-body problem"

 $03/29/2018\colon$ U. of Maryland Dynamic Seminar, "Metric Approach to McGehee blow-up and Marchall's lemma"

08/19/2018: UC Berkeley, Physics, Robert Littlejohn retirement conference, "Stumbling around Shape Space"

09/13/2018: MSRI, Berkeley, Celestial Mechanics Seminar, "Scattering"

09/20/2018: MSRI, Berkeley, Celestial Mechanics Seminar, "Scattering, ct'd"

11/26/2018: MSRI, "Scattering in the N-body problem", a seminar series

11/26/2018: MSRI, Berkeley, final programmatic workshop within the Hamiltonian systems semester; conference titled "Hamiltonian systems, from topology to applications through analysis II", my talk: "Infinitely many coplanarities"

02/13-14-15/2019: U. Jyvaskyla, Finland, a 3 days (6 hour) minicourse for preparing students and participants for the upcoming conference (see next entry). Course title: "Geometric mechanics with applications to subriemannian geometry"

02/19/2019: U. of Jyvaskyla, Finland, 2nd day of week-long conference: SubRiemannian Geometry and Beyond, II, "Elastica, Optimal Rolling, and Wong's equations"

03/01/2019: Groupe de Travail Contrôle, Sorbonne Universit - Paris 6, Paris, "Elastica, optimal rolling, and Wong's equations".

 $03/07/2019\colon$ U. of Grenoble Math. Dept. Colloquium, "Oscillating about coplanarity in the 4 body problem"

04/17/2020: International SubRiemannian Seminar (Zoom), opening talk of year-long seminar series, "Magnetic Playground Fields for Understanding subRiemannian geodesics"

 $06/02/2020{:}$ Geometry, Dynamics and Mechanics Seminar, (international Zoom seminar) "Scattering Bodies"

10/03/2020: AMS Fall Sectional Meeting, (remote) "N body scattering and billiards"

12/03/2020: Vanderbilt U., Dept. Colloquium (by Zoom), "Open Problems within the N-body problem"

06/27-30/2022, Barcelona, 18TH School on Interactions between Dynamical Systems and Partial Differential Equations (JISD2022) a 4-day summer school of an hour to an hour and a half per day, "Variational and Differential Geometry Methods in the N-body Problem"

07/04/2022, Barcelona, Centre de Recerca Matematica, Popcorn Math session, (Eva Miranda's seminar) "Brakes or Infinity - in N-body problems"

11/10/2022: U. of Fribourg, Switzerland, Dept. Colloquium "From falling cats to the N-body problem"

13/10/2022: University of Erlangen-Nürnberg, Mathematical Physics seminar, "Scattering and Compactifying in Newton's three body problem"

18/10/2022: University of Erlangen-Nürnberg, Math Colloquium, "From falling cats to the N-body problem"

 $20/10/2022\colon$ U. of Heidelberg, Workshop on Geometry and Dynamics, "2 Questions for the 3-body problem"

Conferences organized

10/1989.(with Tudor Ratiu) International conference on Geometric Phases, Cornell U., Ithaca, NY.

3/8-12/1989. (with Jair Koiller) of International Workshop on Geometric Mechanics and Control, , IMPA, Rio de Janeiro, Brazil.

5/1997 Minisymposium on microswimming for SIAM Dynamics Days, Park City Utah

7/2000. (with J. Huebschmann) session in Mathematical Physics for the joint American Math.Society-French math Society international congress, Lyon, France.

6/9-6/14/2003: (with A. Chenciner) AIM/ARCC international workshop on Variational Methods in Celestial Mechanics, Palo Alto, CA. (see http://www.aimath.org/ARCC/workshops/varcelest.html)

5/9/2009 (with D. Hoffmann) Bay Area Differential Geometry Seminar, Santa Cruz meeting

01/11-13/2018: AMS Joint Meeting, San Diego, AMS Special Session on New Trends in Celestial Mechanics

Memberships and Refereeing.

Member, American Mathematical Society, Society for Industrial and Applied Mathematics Reviewer for NSF grants

Refereeing: Annals, Inventiones, American J. of Physics, Amer. Math Monthly, Intelligencer, Mathematical Reviews, Communications in Mathematical Physics, Journal of Mathematical Physics, Nonlinearity, Physics Letters A, Journal of Differential Geomety, Nonlinearity, Physics Review Letters, Pacific Journal of Mathematics, SIGMA, RCD, and a number of other journals.

Editorial Boards. Nonlinearity (Associate Editor), SIGMA