

McGehee's counterexample map of the plane is

$$f(x, y) = (x - x^2 + y^2, 2xy)$$

- a) Rewrite f in complex variable terms, so in terms of a single complex variable z . (You are allowed conjugation !)
- b) Establish the equivariance of this map with respect to the cyclic group of three elements which is generated by the third root of unity ω .
- c) Establish that the "stable manifold" of the origin $z = 0$ consists of three rays separated by 120 degrees.
- d) Establish that the "unstable manifold" consists of three rays oriented at 120 degrees.