

HW # 3 Levi 17

Let $\triangle ABC$ have sides with lengths 3, 4, x .

Note that $3+4 > x \Rightarrow 7 > x$

$3+x > 4 \Rightarrow x > 1 \Rightarrow x \in (1, 7)$.

$4+x > 3 \Rightarrow x > -1$

By the lemma, the maximum area of $\triangle ABC$ occurs when $x=5$ in which case the area = 6.

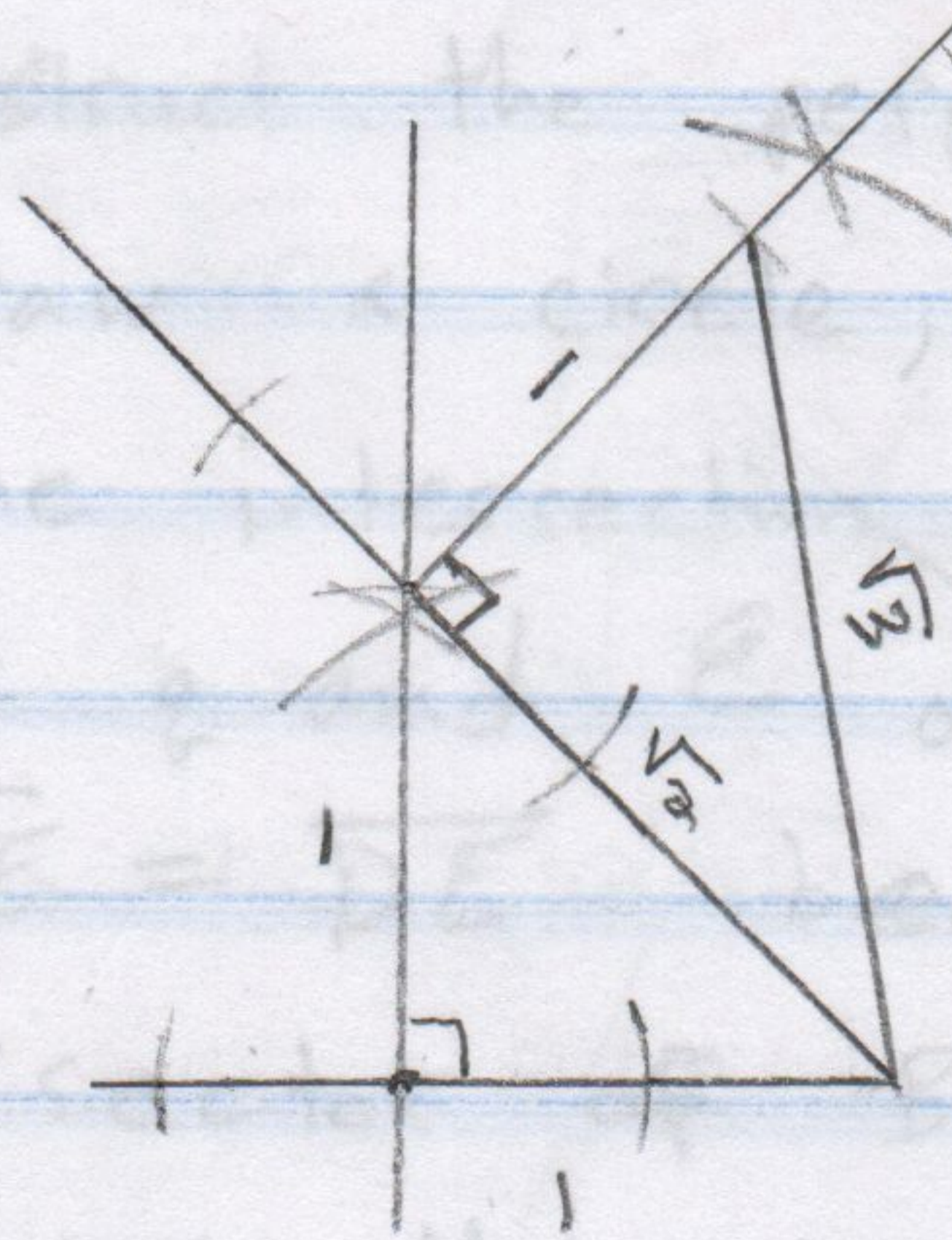
Looking at the diagram and using similar logic to that used in the lemma, it is apparent that the area of $\triangle ABC$ approaches 0 as C approaches the line segment AB in a counter-clockwise direction.

Therefore

Area $\triangle ABC \in (0, 6]$.

5/5

Pillars 2.5.4



4/5

Pillars 2.7.4

Given an n -gon, we may cut up the n -gon into Δ s (by assumption). These Δ s may be "squared" (by Levi 9). These squares may be combined, two squares at a time, into one big square whose area is the sum of the little squares (by 2.7.3).

how?
using what?

$\rightarrow \text{Area } ABTO = \sum \text{Area } \triangle ABC.$

Q.E.D.