1. The problems here were taken from the site 'abetterfilecabinet'.
2. Find the following limits. Be sure to explain your reasoning at each step.
a) $\lim _{x \rightarrow \infty} \frac{x+\sin x}{5 x+6}$
b) $\lim _{x \rightarrow \infty} \frac{\sin x}{x}$
c) $\lim _{x \rightarrow \infty} x \sin \frac{1}{x}$
d) $\lim _{x \rightarrow \infty} \frac{x \sin x}{x^{2}+5}$
e) $\lim _{x \rightarrow \infty} \sqrt{x^{2}+x}-x$
f) $\lim _{x \rightarrow \infty} \frac{x^{2}\left(1+\sin ^{2} x\right)}{(x+\sin x)^{2}}$
3. Compute the following limits algebraically:

$$
\begin{aligned}
& \lim _{x \rightarrow 2} \frac{|x-2|}{x^{2}-2 x} \\
& \lim _{x \rightarrow-1^{+}} \frac{|x+1|}{x^{3}+1} \\
& \lim _{x \rightarrow 2} \frac{(x-2)^{2}}{|x-2|}
\end{aligned}
$$

Note: These are all previous exam problems!
4. (a) For $n=3,4,5$ find the perimeter of an $n$-sided regular polygon (i.e. an equilateral triangle, a square, and a regular pentagon) inscribed in a circle of radius 2 .
(b) Find a general formula for an $n$-sided regular polygon's perimeter (inscribed in a circle of radius 2).
(c) Draw a picture of a circle of radius 2 with a twelve and a 20 -sided regular polygon inscribed.
(d) What is the limit, as $n \rightarrow \infty$ of the formula you found in part (b).
5. Let

$$
f(x)=\frac{x^{2}-1}{x+1}
$$

(a) Sketch the graph of $f(x)$, and determine its domain and range.
(b) Evaluate $f(-1)$ and $f(1)$.
(c) Evaluate

$$
\lim _{x \rightarrow-1} f(x) \quad \text { and } \quad \lim _{x \rightarrow 1} f(x)
$$

6. How long does it take for a sum of money to double when compounded continuously (a) at $6 \%$, (b) at $8 \%$, and (c) at $10 \%$ ?
7. At what rate $r$ of continuous compounding does a sum of money triple in 20 years?
