- 1. The problems here were taken from the site 'abetterfilecabinet'.
- 2. Find the following limits. Be sure to explain your reasoning at each step.

a) 
$$\lim_{x \to \infty} \frac{x + \sin x}{5x + 6}$$
b) 
$$\lim_{x \to \infty} \frac{\sin x}{x}$$
c) 
$$\lim_{x \to \infty} x \sin \frac{1}{x}$$
d) 
$$\lim_{x \to \infty} \frac{x \sin x}{x^2 + 5}$$
e) 
$$\lim_{x \to \infty} \sqrt{x^2 + x} - x$$
f) 
$$\lim_{x \to \infty} \frac{x^2 (1 + \sin^2 x)}{(x + \sin x)^2}$$

3. Compute the following limits algebraically:

$$\lim_{x \to 2} \frac{|x-2|}{x^2 - 2x}$$
$$\lim_{x \to -1^+} \frac{|x+1|}{x^3 + 1}$$
$$\lim_{x \to 2} \frac{(x-2)^2}{|x-2|}$$

Note: These are all previous exam problems!

- 4. (a) For n = 3, 4, 5 find the perimeter of an *n*-sided regular polygon (i.e. an equilateral triangle, a square, and a regular pentagon) inscribed in a circle of radius 2.
  - (b) Find a general formula for an *n*-sided regular polygon's perimeter (inscribed in a circle of radius 2).
  - (c) Draw a picture of a circle of radius 2 with a twelve and a 20-sided regular polygon inscribed.
  - (d) What is the limit, as  $n \to \infty$  of the formula you found in part (b).
- 5. Let

$$f(x) = \frac{x^2 - 1}{x + 1}$$

- (a) Sketch the graph of f(x), and determine its domain and range.
- (b) Evaluate f(-1) and f(1).
- (c) Evaluate

$$\lim_{x \to -1} f(x) \quad \text{and} \quad \lim_{x \to 1} f(x).$$

- 6. How long does it take for a sum of money to double when compounded continuously (a) at 6%, (b) at 8%, and (c) at 10% ?
- 7. At what rate r of continuous compounding does a sum of money triple in 20 years?