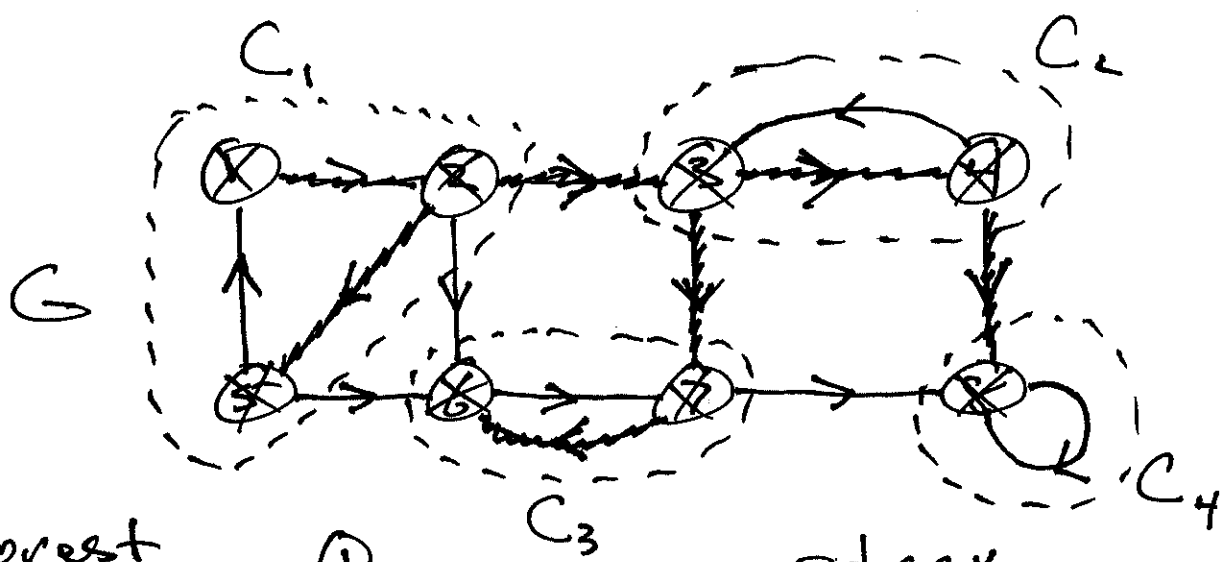


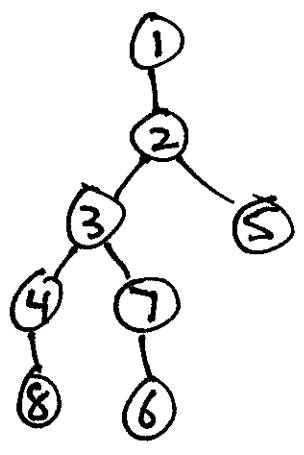
CSE 101 1-29-25

- Midterm 1: Friday 1-31-25
- Pa3: ext. 2 days

Ex. find SCCs :



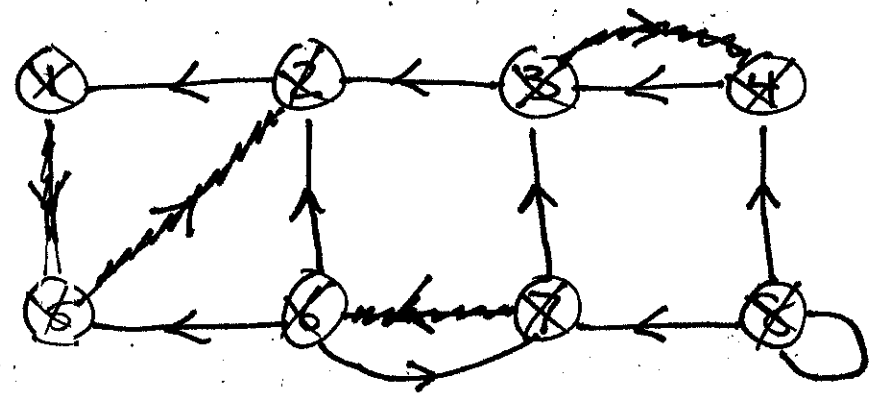
Forest



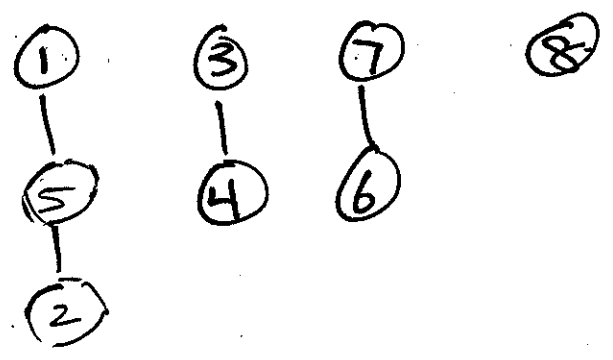
stack

- 1 ✓
- 2 ✓
- 3 ✓
- 7 ✓
- 6 ✓
- 5 ✓
- 8 ✓

G^T



Farrist



<u>stack</u>	<u>p</u>
8	n
7	n
6	
3	n
4	
1	n
5	
2	

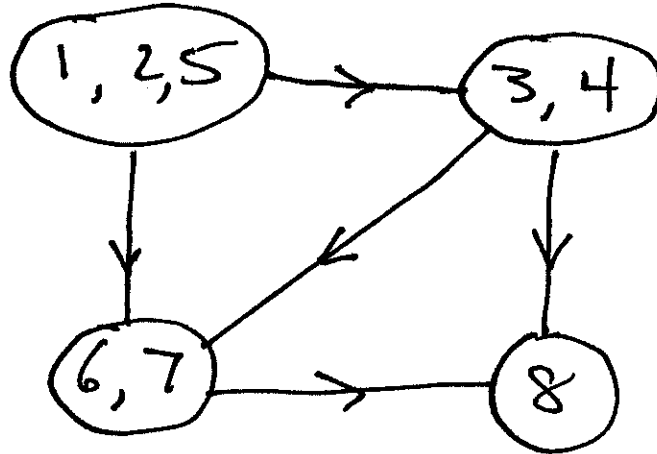
Component graph, Condensation graph

Defn G^{SCC} is the digraph with

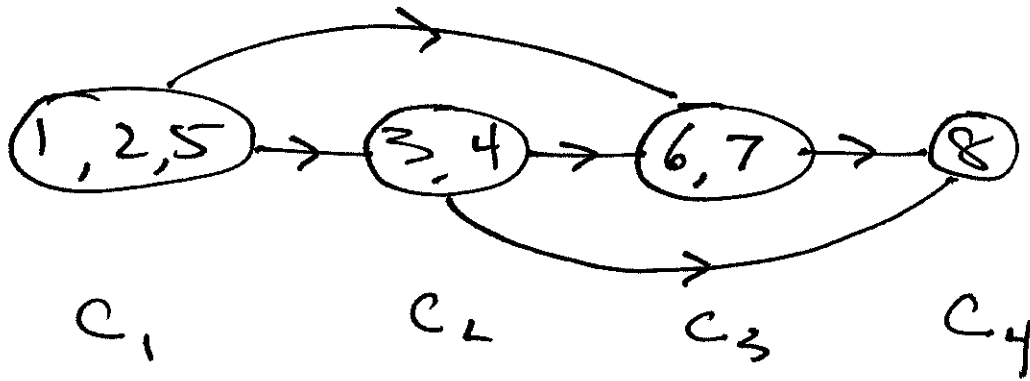
$$V = \{ SCCs \text{ of } G \}$$

$$E = \{ (i, j) \mid \exists x \in C_i, y \in C_j \text{ s.t. } (x, y) \in E(G) \}$$

G_{SCC}



Topological Sort!



Output

- 1 : 1 5 2
- 2 : 3 4
- 3 : 7 6
- 4 : 8

Prepare $S = (1, 2, 3, \dots, n)$



DFS(G, S)



$T = \text{transpose}(G)$



DFS(T, S)



gives you topological sort of SCCs

How to treat S inside DFS, without making copy

- 1
- 2
- ~~3~~
- 4
- ~~5~~
- 6
- 7
- ~~8~~

list section

cursor → 8

- 8
- 7
- 6
- 3
- 4
- 1
- 5
- 2

stack section