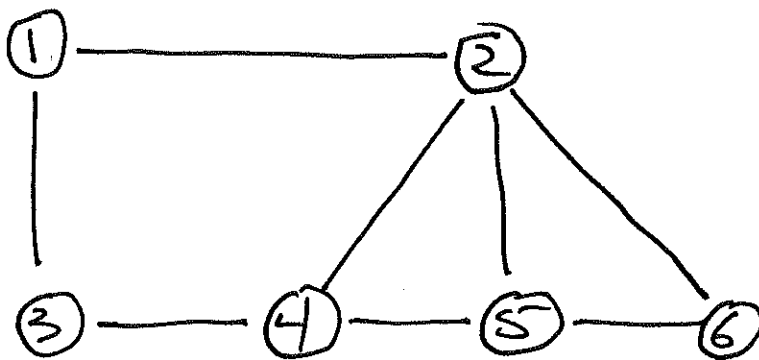


Ex. BFS : S = 3



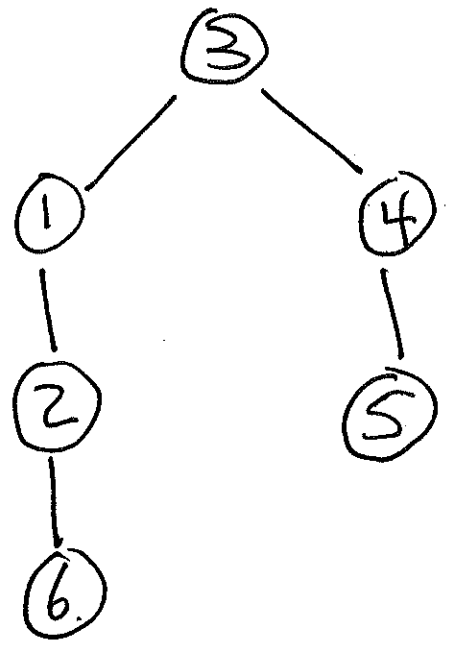
	adj	color	d	P
✓ 1	<u>2</u> , <u>3</u>	w g b	∅ 1	∅ 3
✓ 2	<u>1</u> , <u>4</u> , <u>5</u> , <u>6</u>	w g b	∅ 2	∅ 1
✓ 3	<u>1</u> , <u>4</u>	g b	0	∅
✓ 4	<u>2</u> , <u>3</u> , <u>5</u>	w g b	∅ 1	∅ 3
✓ 5	<u>2</u> , <u>4</u> , <u>6</u>	w g b	∅ 2	∅ 4
✓ 6	<u>2</u> , <u>5</u>	w g b	∅ 3	∅ 2

Q: ~~∅~~ ~~x~~ ~~4~~ ~~∅~~ ~~∅~~ ~~∅~~

Shortest Paths Tree!

or BFS Tree!

dist = depth



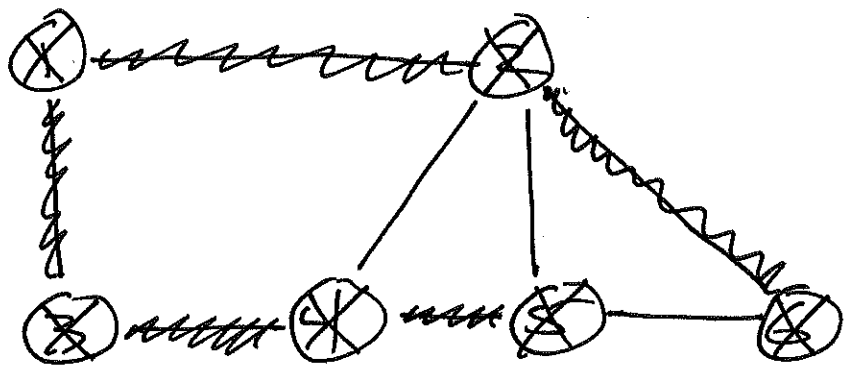
- 0
- 1
- 2
- 3

Also called Predecessor

Subgraph

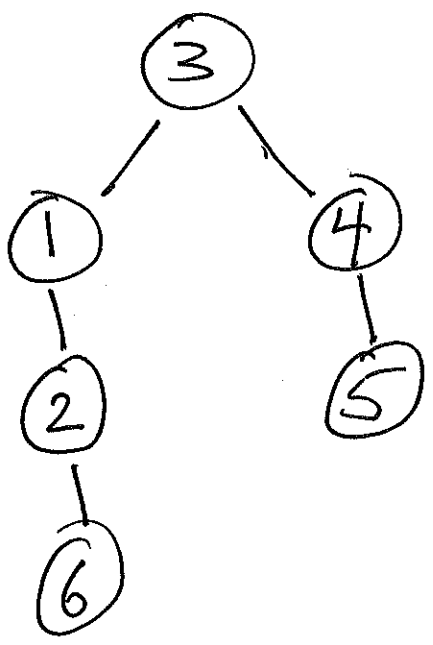
Ex. same (easy way)

$S=3$



Q: 1, 2, 3, 4, 5, 6

BFS Tree:



dist

0

1

2

3

Defn.

The Predecessor Subgraph is

$T = (V_p, E_p)$ where

$$V_p = \{x \in V(G) \mid p[x] \neq \text{nil}\} \cup \{s\}$$

$$E_p = \{ \underbrace{(p[x], x)} \mid p[x] \neq \text{nil} \}$$

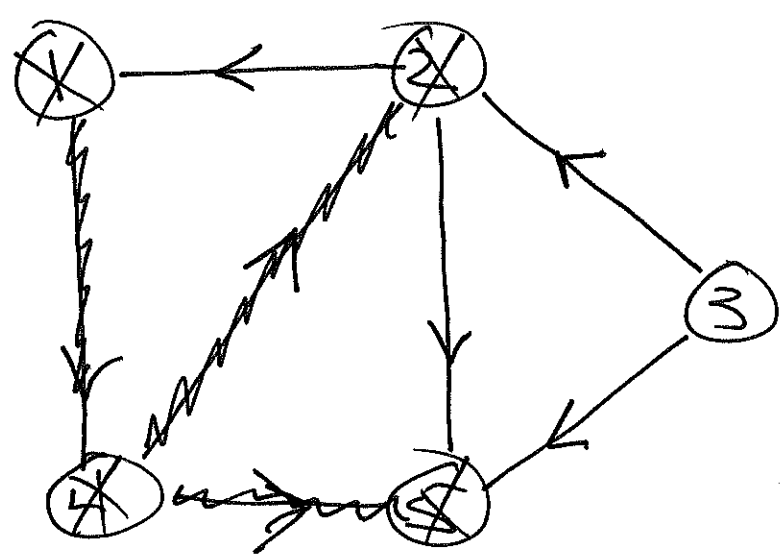
- ordered pair if directed
- unordered $\{p[x], x\}$ if undirected

Note! • T is acyclic

$$\bullet m = n - 1$$

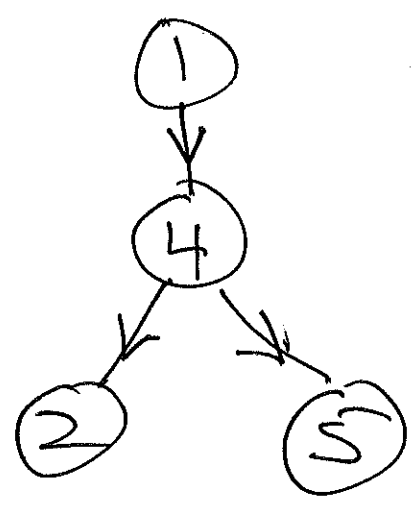
• T is a tree!

Ex. (directed) r=1



Q: 1 4 2 5

BFS Tree



<u>dist</u>
0
1
2