

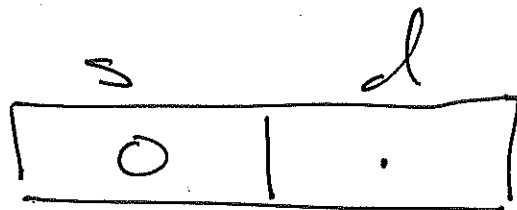
CSE 101-01

5-18-23

11

pag: ext. 2 days  $\rightarrow$  Monday

BigInteger: zero state



( ) empty list

from long constructor:  $x$  is a long

$x > 0$ : signum = 1, digits = (., ., ., ...)

$x < 0$ : signum = -1, digits = (., ., ...)

from string constructor :

S = "1|23|45|67|89|87|65|43"

suppose base = 100, Power = 2

Use : in string.h

substr()

strtol()

also : find\_first\_of()

find\_first\_not\_of()

Ex. normalize & subtraction

let  $p = 2, b = 100$

(13 23 81)

(52 20 92)

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-1 (-39 -1 3 -11) vector sub

100 100

(-1 61 2 89) no-normalize

-1

-1 -1 -1  
(1 -61 -2 -89)

-62 -3  
100 100 100

(∅ 38 97 11)

(38 97 11) no-normalize

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state of no-normalized list

↓  
return

# Dictionary ADT

chapters (CLRS):

- ch 12 : BST
- ch 13 : RBT
- ch 11 : Hash Tables

state a <sup>finite</sup> set of ordered pairs

(key, value)

i.e. a state is a set

$\{(k_1, v_1), (k_2, v_2), \dots, (k_n, v_n)\}$

Require: keys are distinct.

## operations

•  $\text{lookup}(\text{key})$ : return value  
assoc. with key or nil  
if key does not exist

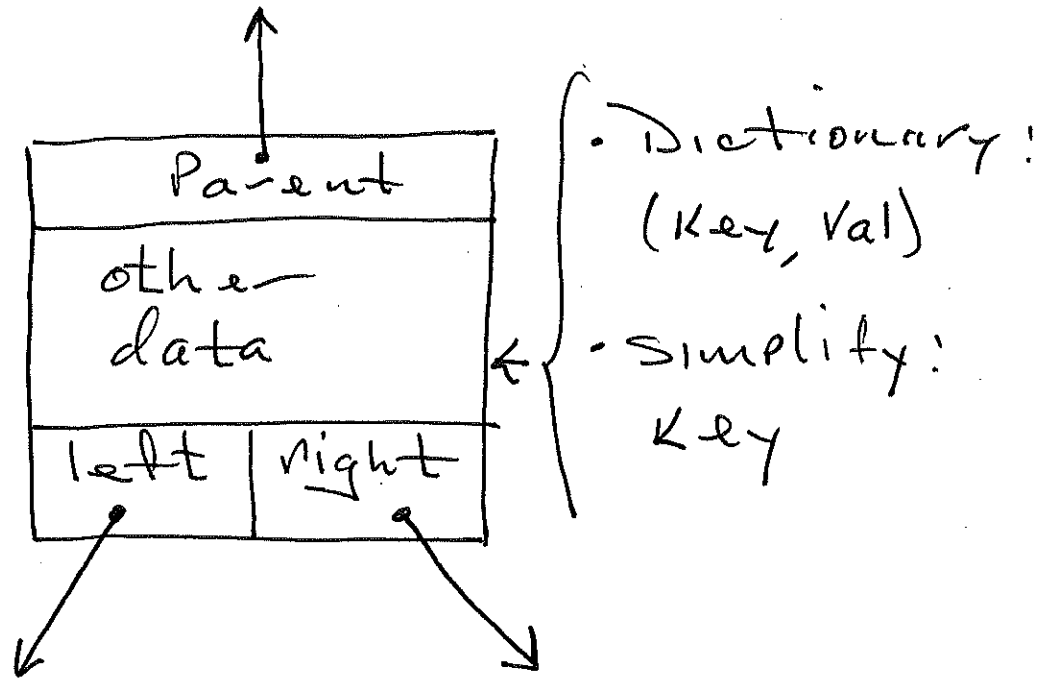
•  $\text{insert}(\text{key}, \text{value})$ : adds a  
new pair to dictionary  
Pre:  $\text{lookup}(\text{key}) = \text{nil}$

•  $\text{delete}(\text{key})$ : remove pair  
from dictionary

Pre:  $\text{lookup}(\text{key}) \neq \text{nil}$

# Binary Search Trees (BST)

## Node Object



## BST Properties

let  $x, y$  be nodes

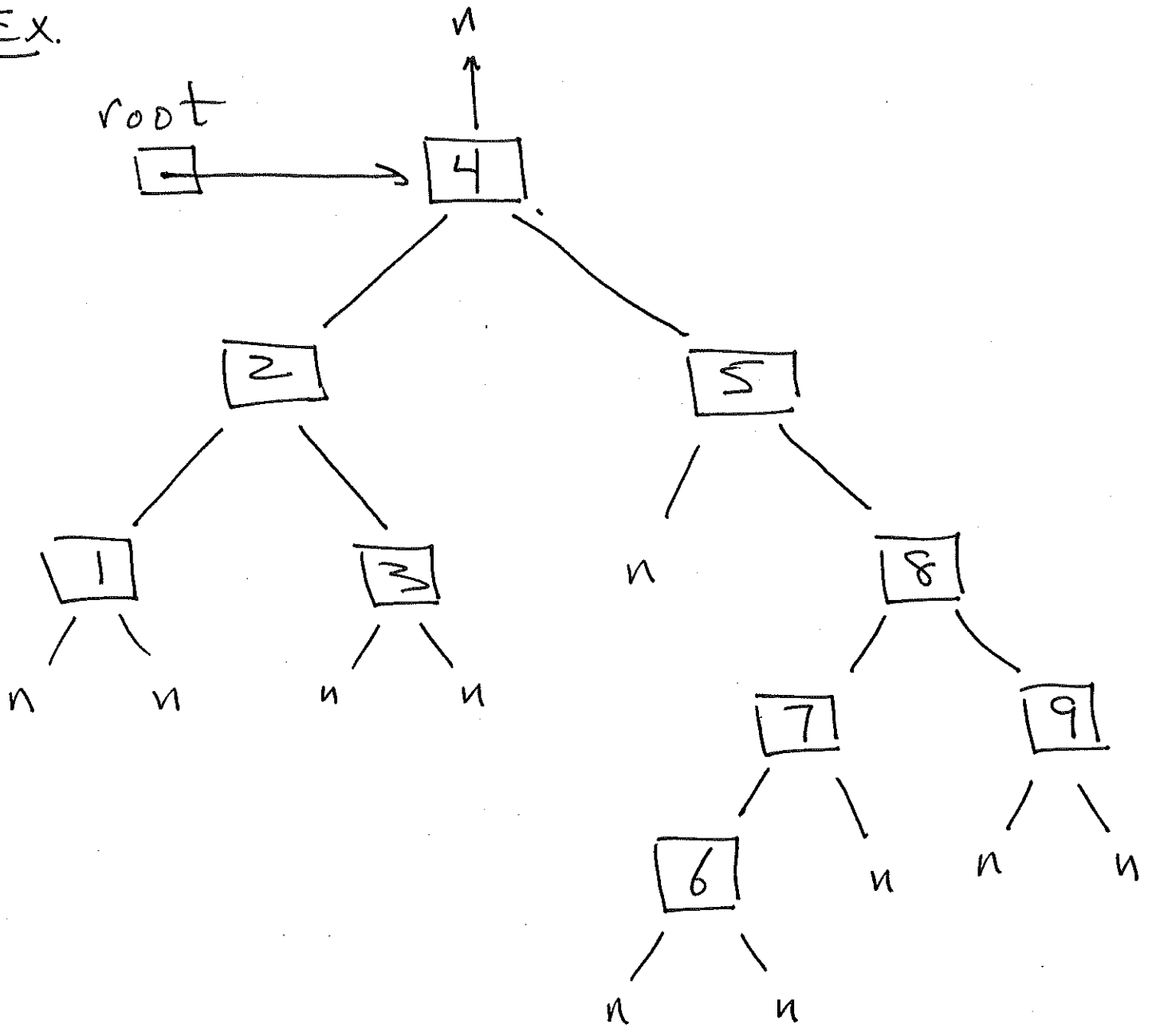
(1) if  $y$  is in left subtree of  $x$ , then

$$\text{key}[y] \leq \text{key}[x]$$

(2) if  $y$  is in right subtree of  $x$ , then

$$\text{key}[x] \leq \text{key}[y]$$

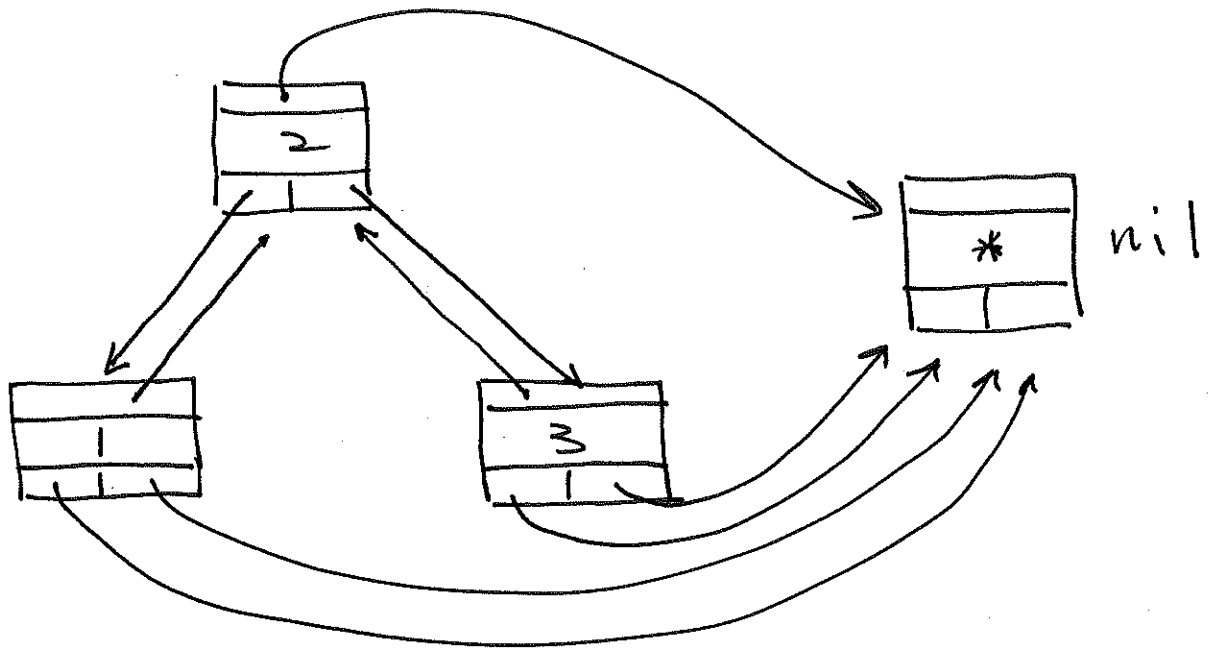
Ex.



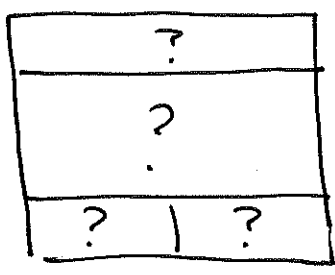
Defn

- a leaf is a node with no children
- an internal node is a non-leaf.

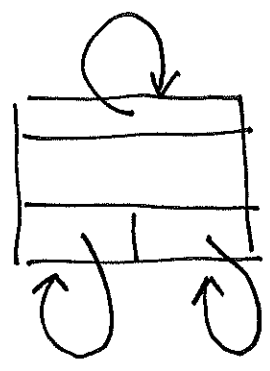
Recommend: dummy nil node



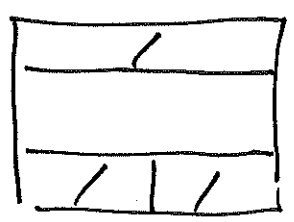
nil:



← what goes here



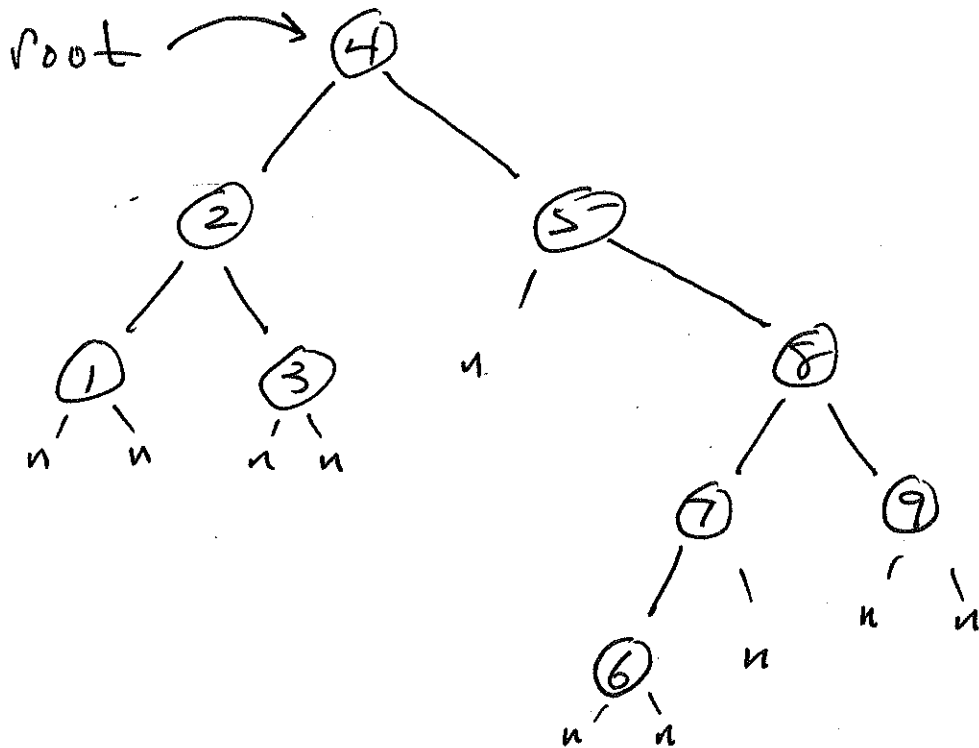
or



# Tree traversals:

- InOrder-TreeWalk(x)
  - ↑ node in a BST
- PreOrder-TreeWalk(x)
- PostOrder-TreeWalk(x)

EX.



IOTW: 1 2 3 4 5 6 7 8 9

Pre OTW: 4 2 1 3 5 8 7 6 9

Post OTW: 1 3 2 6 7 9 8 5 4