

- Pal ext 1 day
- new examples Queue & stack as array.

Exercise

re-create list ADT from Pal based on an Array data structure (use array doubling.)

Graph Theory handout:

A Graph is a pair of sets

$$G = (V, E)$$

where

$$V \neq \emptyset \quad (\text{vertices})$$

$$E \subseteq V^{(2)} = \{ \text{2-element s/sets of } V \}$$

Pic: $\{x, y\}$
 xy



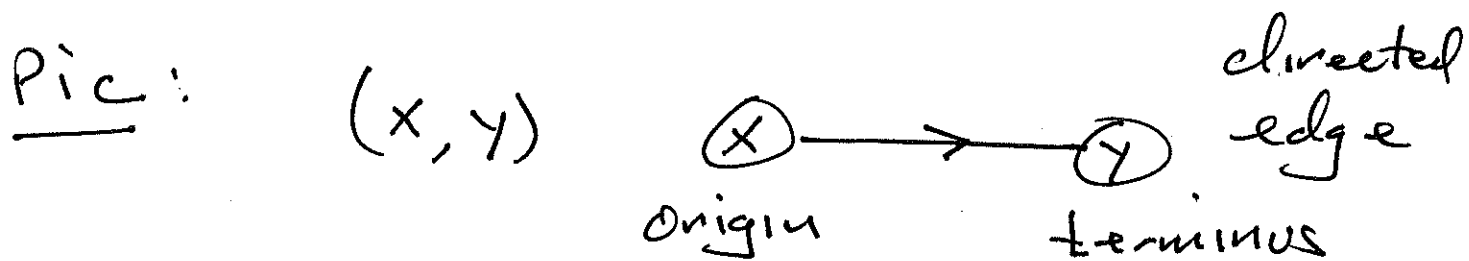
undirected
edge

A Dig-graph is a pair of sets

$$G = (V, E)$$

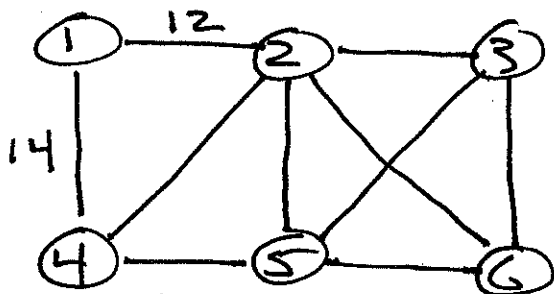
where

$$V \neq \emptyset, \quad E \subseteq V \times V$$



Ex. $V = \{1, 2, 3, 4, 5, 6\}$

$E = \{12, 14, 23, 24, 25, 26, 35, 36, 45, 56\}$



1 is adjacent to 2
ends
join
 12 is incident to 1
 12 is adjacent to 14

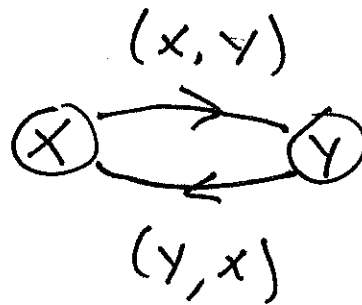
note: in a graph

and

are not allowed



but in a dig-graph:



are allowed.

• Walk from x to y is a sequence

$$x = v_0, v_1, v_2, \dots, v_k = y \quad \left(\begin{array}{l} \text{length} \\ = k \end{array} \right)$$

in which $\{v_{i-1}, v_i\} \in E(G)$ ($1 \leq i \leq k$)

a walk is closed if $x = y$.

- trail is a walk in which no edge is repeated.
- Path is a trail in which no vertex is repeated (except possibly in case $x=y$.)
- length (walk, trail, path) is the # of edge traversals
- a walk trail or path is trivial if $\text{length} = 0$.
- a non-trivial closed path is called a cycle.

We say y is reachable from x iff G contains an x - y Path.

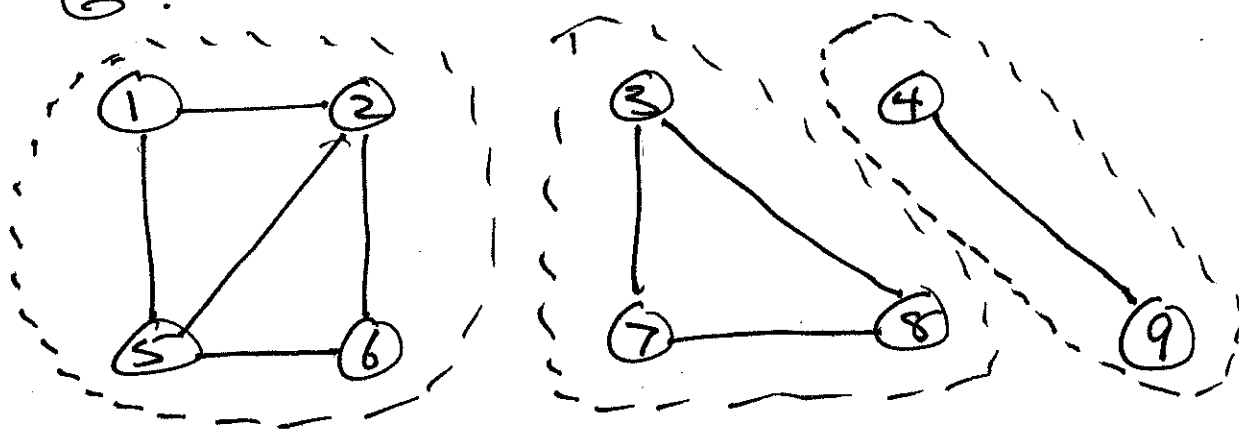
Defn

a graph G is called connected iff for all $x, y \in V(G)$: x is reachable from y , and y is reachable from x .

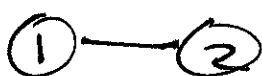
Defn a sub-graph H of G is called a connected component of G iff

- (1) H is connected, and
- (2) H is maximal w.r.t. (1).

Ex. G :

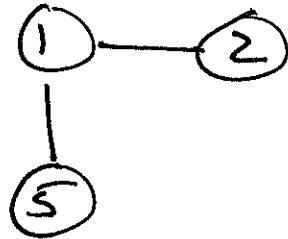


• Sub-graph $(\{1, 2, 5\}, \{12\})$



Disconnected

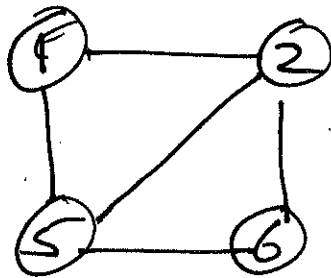
• subgraph $(\{1, 2, 5\}, \{12, 15\})$



connected

not a conn.
comp.

• subgraph $(\{1, 2, 5, 6\}, \{12, 15, 25, 26, 56\})$



connected
maximal

The distance from x to y

$$S(x, y) = \begin{cases} \text{len. of a shortest} \\ x-y \text{ Path, if } y \text{ reachable} \\ \text{from } x \\ \infty \text{ if } y \text{ not reachable} \\ \text{from } x \end{cases}$$