

CSE 101

4-29-21

Pay stvll:

client view:

0	1	2	3	4	5
⋮	⋮	⋮	⋮	⋮	⋮
(2	5	1	3	7	)
⋮	⋮	⋮	⋮	⋮	⋮

inside view

	fd	bc	ac	bd	idx	len
L					3	5

stack

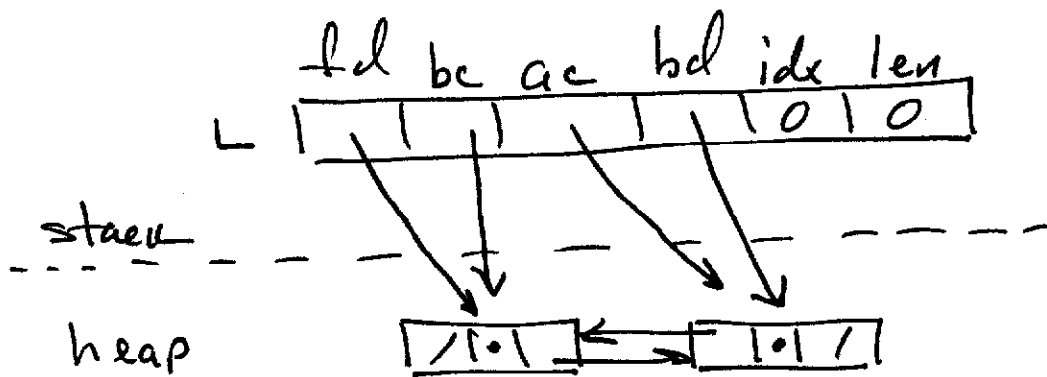
heap



empty state:

client: $\begin{pmatrix} 0 \\ | \end{pmatrix}$

inside:



const. $\frac{1}{2}$ copy const. $\frac{1}{2}$ dest.

→ operator

see! Queue ex.
Stack ex.

Node * N;

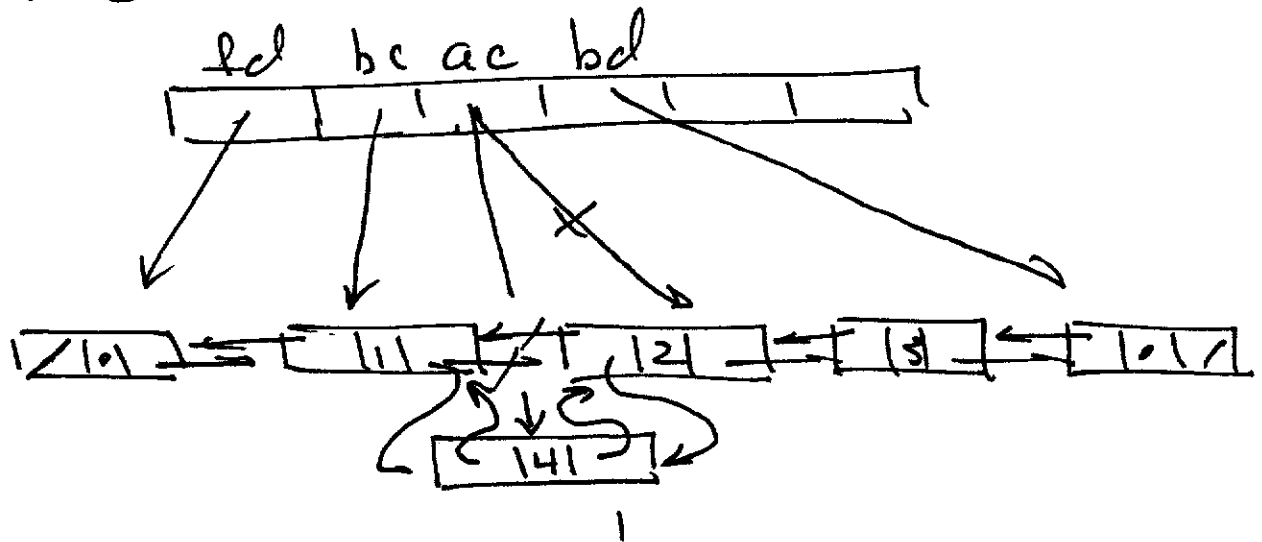
~~*N.next~~

(*N).next equiv to N→next

insertAfter()

client: (1 | 2 3)

inside:



insertAfter(4) : (1 | 4 2 3)

Continue asymp. growth handout

4

Exercises

$$\bullet \quad n^\alpha = \begin{cases} o(n^\beta) & \alpha < \beta \quad \checkmark \\ \Theta(n^\beta) & \alpha = \beta \quad \checkmark \\ \omega(n^\beta) & \alpha > \beta \quad \checkmark \end{cases}$$

Proof:

$$\frac{n^\alpha}{n^\beta} = n^{\alpha-\beta} \xrightarrow[\text{as } n \rightarrow \infty]{} \begin{cases} 0 & \text{if } \alpha < \beta \\ 1 & \text{if } \alpha = \beta \\ \infty & \text{if } \alpha > \beta \end{cases}$$

$$\bullet \quad a^n = \begin{cases} o(b^n) & a < b \\ \Theta(b^n) & a = b \\ \omega(b^n) & a > b \end{cases}$$

- $c f(n) = O(f(n))$
 $\quad \quad \quad = \Theta(f(n))$
 $\quad \quad \quad = \Omega(f(n))$

for any $c > 0$

- $\log_b(n) = \Theta(\log_a(n))$

for any $a > 1, b > 1$.

- if $\lim_{n \rightarrow \infty} \left(\frac{f(n)}{g(n)} \right) = L$, then

a. $L = 0 \iff f(n) = o(g(n))$

b. $0 \leq L < \infty \implies f(n) = O(g(n))$

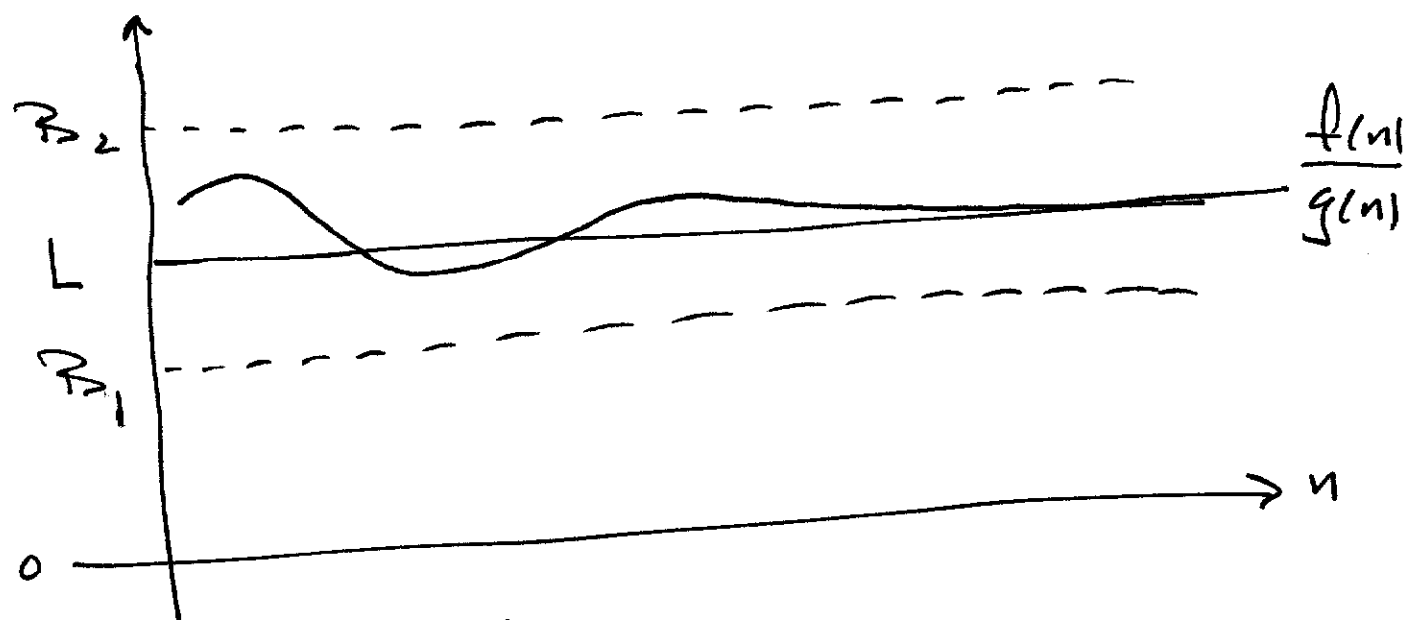
c. $0 < L < \infty \implies f(n) = \Theta(g(n))$

d. $0 < L \leq \infty \implies f(n) = \Omega(g(n))$

e. $L = \infty \iff f(n) = \omega(g(n))$

~~$\iff$~~

look at case c:



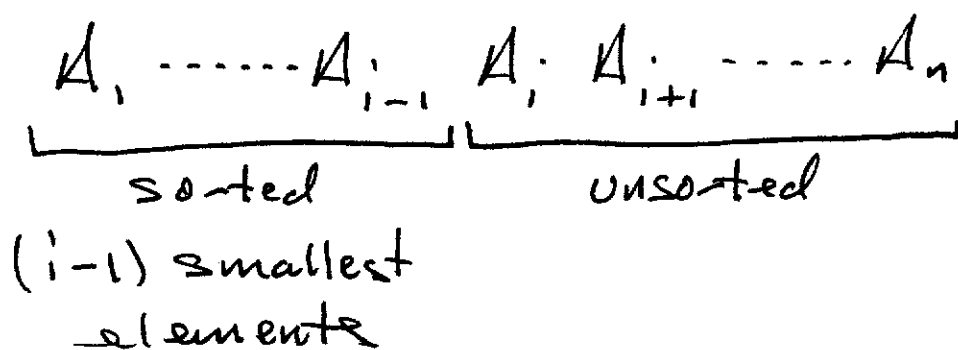
$$\lim_{n \rightarrow \infty} \left(\frac{f(n)}{g(n)} \right) = L$$

• rank the following functions:

$$\left\{ n^2, \ln(n), (\ln n)^2, \ln(n^2), n \ln(n), \sqrt{n}, n\sqrt{n}, \ln(\ln(\sqrt{n})), 2^{\ln(n)}, 2^n, 2^{3^n}, 3^{2^n} \right\}$$

Selection Sort (A)

1. $n = \text{length}[A]$
2. for $i = 1$ to $n-1$
3. $i_{\min} = i$
4. for $j = i+1$ to n
5. if $(A[j] < A[i_{\min}]) \leftarrow \text{basic op.}$
6. $i_{\min} = j$
7. $A[i] \leftrightarrow A[i_{\min}]$ // swap



Basic Operation in Sorting Algorithm:

Comparison of array elements

(# comparisons as a fun of n)

	<u># comp</u>
$i = 1$	$n-1$
$i = 2$	$n-2$
$i = 3$	$n-3$
$\vdots$	
$i = n-1$	1

$$\# \text{comp} = 1 + 2 + 3 + \dots + (n-3) + (n-2) + (n-1)$$

$$= \frac{n(n-1)}{2} = \frac{n^2 - n}{2}$$

$$= \frac{1}{2}n^2 - \frac{1}{2}n = \underbrace{\Theta(n^2)}$$

best, worst and avg !!

next time:

BFS, DFS routines.