## MATHEMATICS FOR ECONOMICS

## Problem Set 5

The problems came from Simon and Blume (1994).
Chapter 21: 2, 5, 8, 9, 11, 12, 15
In addition, you are asked to answer the following open question in Note 5

1. Show that $[\mathrm{a}, \mathrm{b}] \times[\mathrm{a}, \mathrm{b}] \subset \mathbb{R}^{2}$ is a convex set.
2. Prove Theorem 5 for $\mathrm{H}^{+}$.
3. Use Definition 7 to show that $f(x)=-x^{2}$ is a concave function on $\mathbb{R}$.
4. Use Theorem 8 to show that $f(x)=-x^{2}$ is a concave function on $\mathbb{R}$.
5. Use Theorem 9 to show that $f(x)=-x^{2}$ is a concave function on $\mathbb{R}$.
6. Prove that the upper level sets of $f(x)=-|x|$ are convex sets.
7. Complete Example 2.
