

**Midterm 3 – 65 Points**

You must answer all questions. Please write your name on every page. The exam is closed book and closed notes. You may use calculators, but they must not be graphing calculators. No cell phones. Do not use your own scratch paper.

**You must show your work to receive full credit**

*I have neither given nor received unauthorized aid on this examination, nor have I concealed any similar misconduct by others.*

Signature \_\_\_\_\_

**Problem 1 (50 Points)**

Suppose that you wish to predict wage outcomes via the following specification:

$$\log(\text{wage}) = \beta_0 + \beta_1 \text{educ} + \beta_2 \text{exper} + \beta_3 \text{tenure} + \beta_4 \text{Sibs} + \beta_5 \text{Brthord} + \beta_6 \text{feduc} + \beta_7 (\text{meduc} + \text{feduc}) + u$$

*wage* is measured in dollars per month, *educ*, *exper*, *tenure*, *meduc* (mother’s education) and *feduc* (father’s education) are measured in years. *Sibs* measures number of siblings, and *Brthord* measures the order in which the respondent was born (1=first, 2=second, etc). The results from estimating this equation are below:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	5.4707580	0.1413698	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
educ	0.0620606	0.0080466	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
exper	0.0185869	0.0040521	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
tenure	0.0096864	0.0030322	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
sibs	0.0017676	0.0080854	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
brthord	-0.0168955	0.0121860	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
feduc	-0.0006832	0.0105281	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
I(meduc + feduc)	0.0119228	0.0065391	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx

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 Residual standard error: 0.3745 on 655 degrees of freedom  
 Multiple R-squared: 0.1835, Adjusted R-squared: 0.1748  
 F-statistic: 21.03 on 7 and 655 DF, SSR = 91.84

a.) Please construct and interpret a 95% confidence interval for the coefficient on *educ*. (10 Points)

b.) Using the 93% confidence level, test whether the coefficient on *tenure* is significantly different from zero. Please state your null and alternative hypotheses, and briefly interpret the result. **(10 Points)**

c.) Suppose that I claim that mother's education has a significant effect on wages. What is the probability that I'm wrong? Please state the null and alternative hypotheses, and show your work! **(10 Points)**

d.) Using the 99% confidence level, please test the hypothesis that the effect of *feduc* is significantly different than the effect of *meduc*. Please state your null and alternative hypotheses, and show your work! **(10 Points)**

e.) The variables *Sibs* and *Brthord* take on only integer values, and thus taking derivatives is a bit coarse. So, you decide to leave them out and see what happens to other estimates. The results are below:

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	5.403359	0.129296	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
educ	0.062781	0.007983	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
exper	0.018796	0.004041	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
tenure	0.009691	0.003032	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
feduc	-0.001786	0.010475	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx
I(meduc + feduc)	0.013567	0.006404	xxxxxxxxxxxxxxxxxxxx	xxxxxxxxxxxxxxxxxxxx

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Residual standard error: 0.3745 on 657 degrees of freedom  
Multiple R-squared: 0.1806, Adjusted R-squared: 0.1744  
F-statistic: 28.96 on 5 and 657 DF, SSR = 92.17

Do the variables *Sibs* and *Brthord* have a joint effect on wages? Please state your null and alternative hypotheses, and test the null against the alternative at the 95% level. **(10 Points)**

**Problem 2 (15 Points)**

The *Residential Energy Consumption Survey* is put out by the US Department of Energy every few years. It surveys a representative sample of residents, their energy use, their appliance ownership, and their characteristics (income, family size, etc...). Using the 2005 version of the survey, and restricting the sample to California residents, I estimate the following equation:

$$\log(KWH) = \beta_0 + \beta_1 \log(Income) + \beta_2 Size + u$$

Here, *KWH* is kilowatt-hours of energy consumption, *Income* is household income, and *Size* is the number of people in the household. The results from estimating the above equation are as follows:

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Coefficients:
              Estimate Std. Error  t value Pr(>|t|)
(Intercept)  5.52078    0.38881  xxxxxxxxxxxxxxxxxxxxxx
log(Income)  0.26806    0.03710  xxxxxxxxxxxxxxxxxxxxxx
Size         0.09560    0.01719  xxxxxxxxxxxxxxxxxxxxxx
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Residual standard error: 0.5533 on 405 degrees of freedom
Multiple R-squared: 0.1929, Adjusted R-squared: 0.1889
F-statistic: 48.4 on 2 and 405 DF, SSR = 123.97
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a.) Do the variables of the model explain  $\log(KWH)$ ? Please state your null and alternative hypotheses, and test the null against the alternative at the 95% level (**5 Points**).

b.) I wish to predict energy consumption for a family that earns \$100,000 a year and has 5 people in the household. Please derive a new equation that allows me to generate this prediction and a standard error for the prediction. Show your work!!! **(10 Points)**



## Normal Distribution from $-\infty$ to $Z$

$Z$	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990