Homework Assignment 3 – Solutions

October 20, 2013

1 List splits

```
ghci 1> let \{split :: [a] \to [([a], [a])];

split [] = [([], [])];

split (x : xs) = ([], x : xs) : [(x : ys, zs) | (ys, zs) \leftarrow split xs]\}
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ghci 2> split [1..5]

[([],[1,2,3,4,5]),([1],[2,3,4,5]),([1,2],[3,4,5]),([1,2,3],[4,5]),([1,2,3,4],[5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,4,5]),([1,2,3,
```

2 List permutations

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ghci 3> let { perm :: [a] \rightarrow [[a]];

perm [] = [[]];

perm (x:xs) = [ys ++ [x] ++ zs | perm_xs \leftarrow perm xs, (ys,zs) \leftarrow split perm_xs]}
```

```
ghci 4> perm [1..5]
                                       [[1,2,3,4,5],[2,1,3,4,5],[2,3,1,4,5],[2,3,4,1,5],[2,3,4,5,1],[1,3,2,4,5],[3,1,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5],[3,2,4,5]
                                       [1,4,5], [3,2,4,1,5], [3,2,4,5,1], [1,3,4,2,5], [3,1,4,2,5], [3,4,1,2,5], [3,4,2,1,5], [3,4,2,5,5]
                                       1, [1,3,4,5,2], [3,1,4,5,2], [3,4,1,5,2], [3,4,5,1,2], [3,4,5,2,1], [1,2,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3,5], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4,3], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,4], [2,1,
                                       \{4,1,3,5\}, [2,4,3,1,5], [2,4,3,5,1], [1,4,2,3,5], [4,1,2,3,5], [4,2,1,3,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,3,1,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,3,5], [4,2,2,2,2], [4,2,2,2,2], [4,2,2,2,2], [4,2,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,2,2], [4,2,
                                       5, 1], [1, 4, 3, 2, 5], [4, 1, 3, 2, 5], [4, 3, 1, 2, 5], [4, 3, 2, 1, 5], [4, 3, 2, 5, 1], [1, 4, 3, 5, 2], [4, 1, 3, 5, 2],
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                                       [3,1,2],[5,4,3,2,1]
```

```
ghci 5> length (perm [1..5])
120
```

3 Permutations of texts

Display 10 permutations of the words in the second sentence of the following text (from the Penn Treebank, WSJ section):

```
ghci 7> let ws_sent2 = words ((lines text) !! 1)
```

ghci 8> take 10 (perm ws_sent2) [["Mr.","Vinken","is","chairman","of","Elsevier","N.V.",","the","Dutch", "publishing","group","."],["Vinken","Mr.","is","chairman","of","Elsevier", "N.V.",","the","Dutch","publishing","group","."],["Vinken","is","Mr.", "chairman","of","Elsevier","N.V.",","the","Dutch","publishing","group", "."],["Vinken","is","chairman","Mr.","of","Elsevier","N.V.",","the","Dutch", "publishing","group","."],["Vinken","is","chairman","of","Mr.","Elsevier", "N.V.",","the","Dutch","publishing","group","."],["Vinken","is","chairman", "of","Elsevier","Mr.","N.V.",","the","Dutch","publishing","group","."], ["Vinken","is","chairman","of","Elsevier","N.V.","Mr.",","the","Dutch", "publishing","group","."],["Vinken","is","chairman","of","Elsevier","N.V.",",", "mr.","the","Dutch","publishing","group","."],["Vinken","is","chairman","of", "Elsevier","N.V.",",","the","Mr.","Dutch","publishing","group","."],["Vinken", "is","chairman","of","Elsevier","N.V.",",","the","Dutch","Mr.","publishing", "group","."]]

```
ghci 9> take 5 (drop 500 (perm ws_sent2))

[["chairman", "of", "Vinken", "Elsevier", "is", "N.V.", "Mr.", ", ", "the", "Dutch",
    "publishing", "group", "."], ["chairman", "of", "Vinken", "Elsevier", "is", "N.V.",
    ",", "Mr.", "the", "Dutch", "publishing", "group", "."], ["chairman", "of", "Vinken",
    "Elsevier", "is", "N.V.", ", "the", "Mr.", "Dutch", "publishing", "group", "."],
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    "publishing", "group", "."], ["chairman", "of", "Vinken", "Elsevier", "is", "N.V.",
    ",", "the", "Dutch", "publishing", "Mr.", "group", "."]]
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ghci 10> take 5 (drop 20000 (perm ws_sent2))
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    "the","Dutch","is","publishing","Mr.","group","."]]
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