

Math 11B FALL 2007
MIDTERM 1 REVIEW PROBLEMS

1.

- a. Express the Riemann sum as a definite integral from $[-\pi, 3\pi]$.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{\sin(x_k)}{1+x_k} \Delta x$$

- b. Express the following as a Riemann sum using the definition of the definite integral.

$$\int_{-3}^5 \frac{x^2}{1+x^3} dx$$

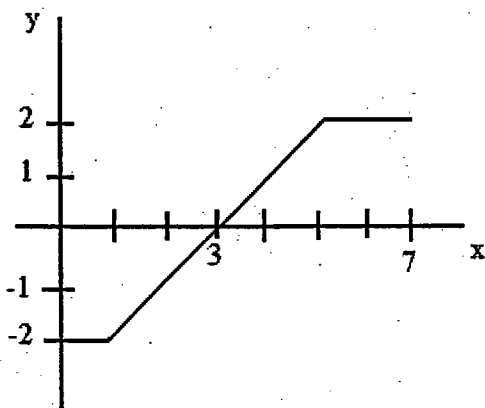
2.

- a. Approximate the area under $y = x^2 + 1$ from 0 to 3 using three equal subintervals and right endpoints.
- b. Approximate the following definite integral using left endpoints and four equal subintervals.

$$\int_1^5 \ln(x) dx$$

3.

- a. Use a geometric argument to calculate $\int_0^7 f(x) dx$ given the graph of $y = f(x)$.



- b. Find the average value of $f(x)$ on $[0, 7]$.

4. Suppose $f(x) = \ln(x)$ represents the path of a particle.

- a. Setup an integral describing the length of the path that the particle travels, $L(t)$, on $[0, t]$.
- b. Find the instantaneous rate of change, $R(t)$, of $L(t)$ (i.e. $\frac{dL(t)}{dt}$).

5. Find the antiderivatives of the following functions.

a. $f(x) = \frac{x^2 + 1 + x}{(x^2 + 1)x}$

b. $g(x) = \frac{1}{2 + 32x^2}$

c. $h(x) = \frac{1-x^2}{\sqrt{(1-x^2)^3}} + \csc(x) \cot(x)$

d. $p(x) = (3e^x)e^{2x} + e^x e^{-x} + \frac{5}{2}(e^{-x})^5$

6. Find the length of $y^{1/3} = \sqrt{x^2 + \frac{6}{9}}$ from $x=0$ to $x=1$.

7. Find the area bounded by $y = \cos(x)$ and $y = \frac{2}{\pi}x + 1$. *IN THE 2ND QUADRANT*

8. Evaluate the following definite integrals.

a. $\int_{\frac{\sqrt{2}}{2}}^{\frac{\sqrt{3}}{2}} \frac{4}{\sqrt{1-x^2}} dx$

b. $\int_1^2 \frac{2}{3x+1} dx$

c. $\int_0^{\pi} (\sin(x) + \cos(x)) dx$

9. Let $\frac{dL}{dt} = \sqrt{2t+4}$

- a. Find $L(t)$ given $L(0) = 98$.
- b. Find the net change from $[6, 16]$.