## CMPS 201 Spring 2010 Homework Assignment 8

1. (1 Point) Give an adversary argument showing that at least  $\binom{n}{2}$  adjacency questions are necessary

(in worst case) to determine whether a graph G on n vertices is acyclic. (Recall by "adjacency" question, we mean a question of the form: "is vertex u adjacent to vertex v".)

- 2. (2 Points) Let  $b = x_1 x_2 x_3 x_4 x_5$  be a bit string of length 5, i.e.  $x_i \in \{0,1\}$  for  $1 \le i \le 5$ . Consider the problem of determining whether *b* contains three consecutive ones, i.e. whether or not *b* contains the substring 111. We restrict our attention to those algorithms whose only allowable operation is to peek at a bit. Obviously 5 peeks are sufficient. A decision tree argument provides the (useless) fact that at least one peek is necessary.
  - a. (1 Point) Give an adversary argument to show that 4 peeks are necessary in general.
  - b. (1 Point) Design an algorithm which solves the problem using only 4 peeks in worst case. Express your algorithm as a decision tree.